

SERIES: TRENDS IN MECHANICS OF MATERIALS

# **OPTICAL BEAMS AT DIELECTRIC INTERFACES**

## **- fundamentals**

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# **Contents**

<b>Preface</b>	<b>vii</b>
<b>1 Introduction</b>	<b>1</b>
References, 13	
<b>2 Basic framework of first-order optics</b>	<b>20</b>
2.1 Introduction, 20	
2.2 Paraxial wave equation, 21	
2.3 Beam amplitude and polarization, 28	
2.4 Hamilton's canonical equations, 31	
2.5 Ray-transfer matrices, 35	
2.6 Optical canonical transforms, 40	
2.7 Hermite-Gaussian beams, 47	
2.8 Laguerre-Gaussian beams, 53	
2.9 Spinors of beam polarization, 57	
2.10 Lorentz transformations, 64	
2.11 Comments and conclusions, 68	
Appendix 1: Note on the scaling, 71	
Appendix 2: Note on the notation, 74	
References, 76	

<b>3 Beam reflection at dielectric interfaces</b>	<b>82</b>
3.1 Introduction, 82	
3.2 Exact analysis, 84	
3.3 Paraxial approximation, 91	
3.4 Paraxial cross-dimensional coupling, 96	
3.5 Nonparaxial cross-polarisation coupling, 97	
3.6 Longitudinal nonspecular effects, 99	
3.7 Transverse nonspecular effects, 100	
3.8 Nonlinear interfaces, 105	
3.9 Beam amplitude nonspecular modifications, 107	
3.10 Comments and conclusions, 110	
Appendix: Geometrical effects of nonspecular reflection, 112	
References, 122	
<b>4 Beam reflection at a nonlinear-linear interface</b>	<b>126</b>
4.1 Introduction, 126	
4.2 Formulation of the problem, 128	
4.3 Derivation of the reflection coefficient, 136	
4.4 Evaluation of the beam field at the interface, 137	
4.4.1 G-o approximation to the reflected field, 137	
4.4.2 Parabolic approximation to the reflected field, 138	
4.4.3 Effects of nonspecular reflection, 139	
4.4.4 Exact evaluation of the reflected field, 140	
4.5 Bistability of nonspecular reflection, 143	
4.6 Comments and conclusions, 147	
Appendix: Aberrationless effects of nonlinear propagation, 149	
References, 158	

<b>5 Amplitude-polarization representation of beams at a dielectric interface</b>	<b>161</b>
5.1 Introduction, 161	
5.2 Beam fields at a dielectric interface - an exact solution, 164	
5.3 First-order optics of beam reflection and refraction, 170	
5.4 Amplitude-polarization decomposition of beam fields, 174	
5.5 New definitions of the nonspecular effects, 176	
5.6 Comments and conclusions, 181	
References, 187	
<b>6 Beams at multilayers - formulation of the problem</b>	<b>189</b>
6.1 Introduction, 189	
6.2 Transmission and reflection matrices, 192	
6.3 Amplitude-polarization spectral decomposition, 199	
6.4 Spinor representation of beam polarization, 201	
6.5 Polarization matrices and Stokes vectors, 205	
6.6 Scattering and transfer matrices, 207	
6.7 Anti-reflection multilayer, 211	
6.8 Comments and conclusions, 213	
References, 217	
<b>7 Spatial distribution versus polarization of beam fields at a planar isotropic interface</b>	<b>219</b>
7.1 Introduction, 219	
7.2 Action of the interface in a spectral domain, 223	
7.2.1 Beam transmission, 225	

7.2.2	Beam reflection, 227
7.3	Normal versus critical incidence of beams, 229
7.3.1	Field decomposition in the linear polarization basis, 229
7.3.2	Field decomposition in the circular polarization basis, 230
7.4	Action of the interface in a spatial domain, 232
7.4.1	The fundamental Gaussian beam, 233
7.4.2	Elegant Hermite-Gaussian modes at the interface, 235
7.4.3	Elegant Laguerre-Gaussian modes at the interface, 239
7.4.4	Beam normal modes at the interface, 250
7.5	Angular momentum of beams at the interface, 251
7.6	Comments and conclusions, 254
	Appendix: One more note on the beam shifts, 255
	References, 268

<b>Subject Index</b>	<b>271</b>
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<b>Author Index</b>	<b>277</b>
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