

# Step meandering

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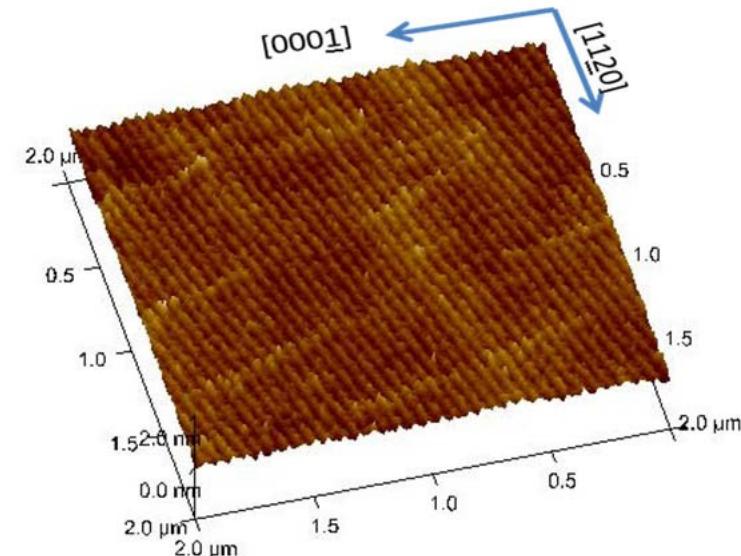
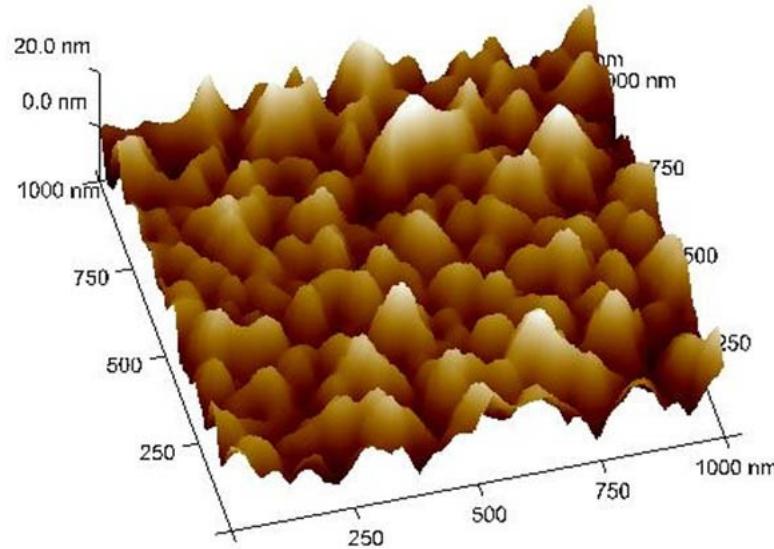
Stanisław Krukowski

Instytut Wysokich Ciśnień PAN

# Crystal growth

We want to reach best control over

- growth mode of the crystal
  - smooth, regular formation of monocrystal
- creation of desired surface structures



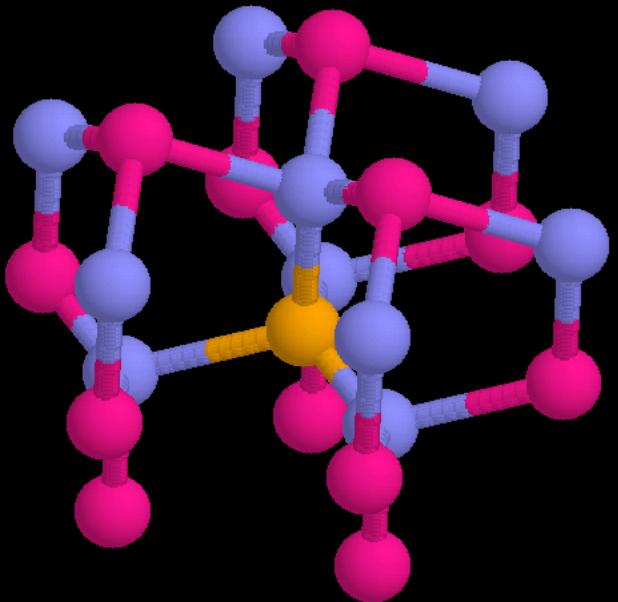
# GaN(0001) surface



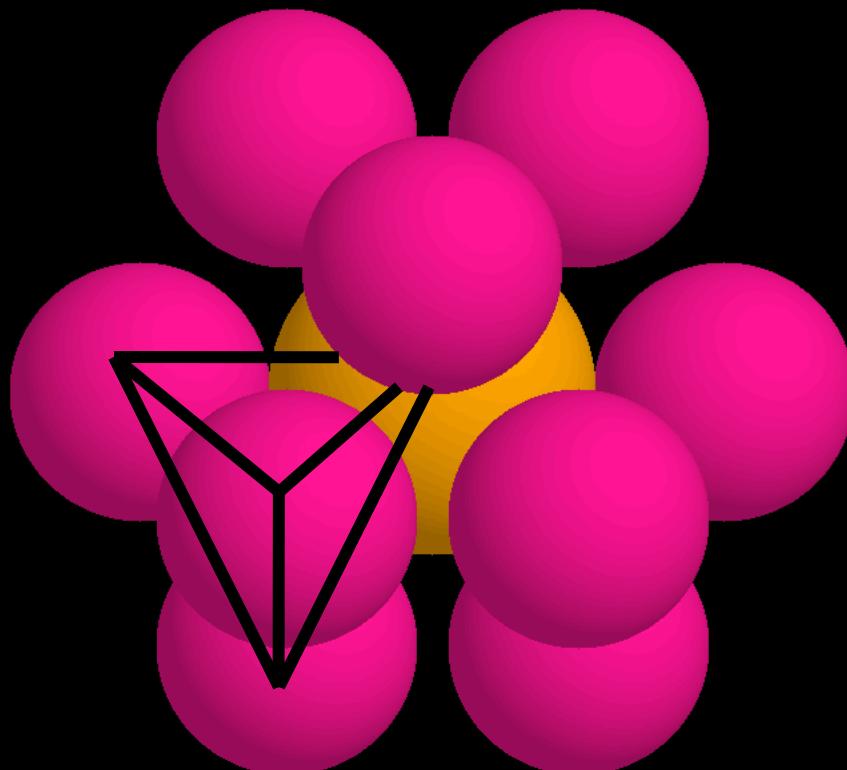
GaN

AFM picture of MOVPE grown GaN layers  
Grzegorz Nowak, Institute of High Pressure Physics (UNIPRESS)  
PAS

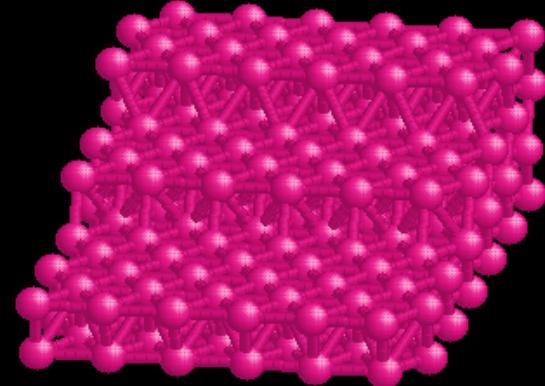
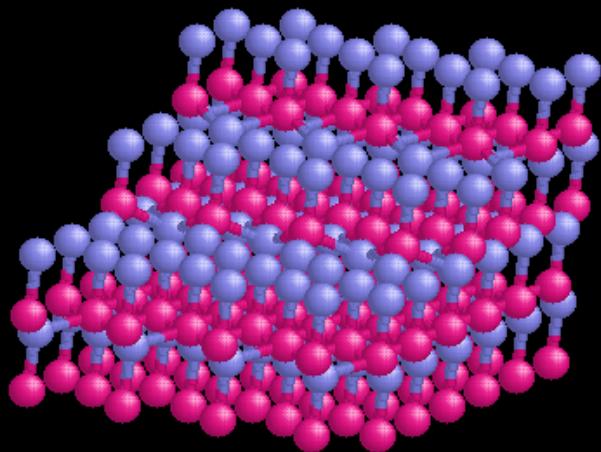
# GaN structure – need for many-particle interactions



# Ga - Ga interaction



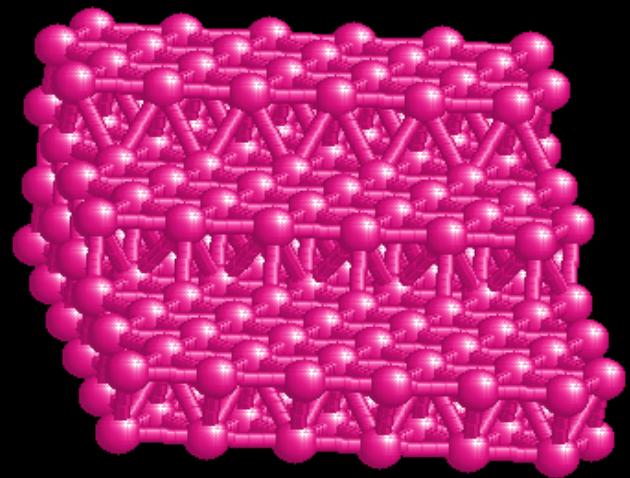
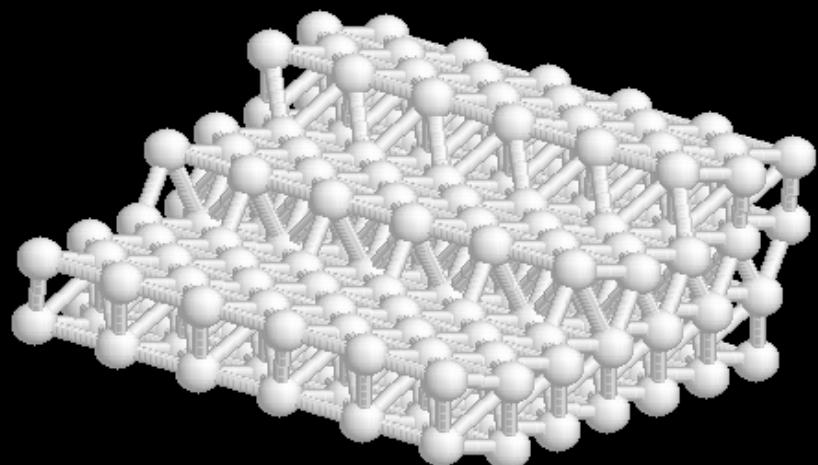
# Structure of GaN(0001) surface



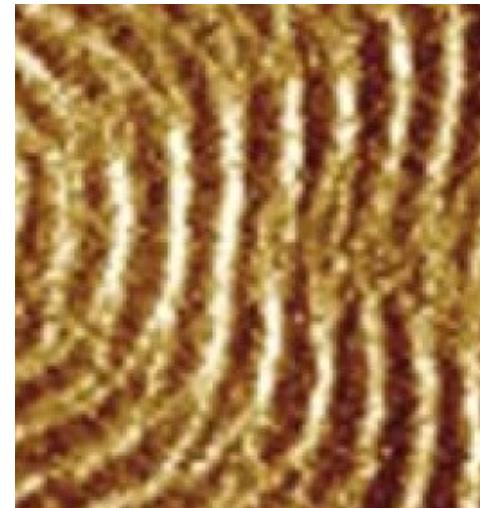
Ga &  
N

Ga

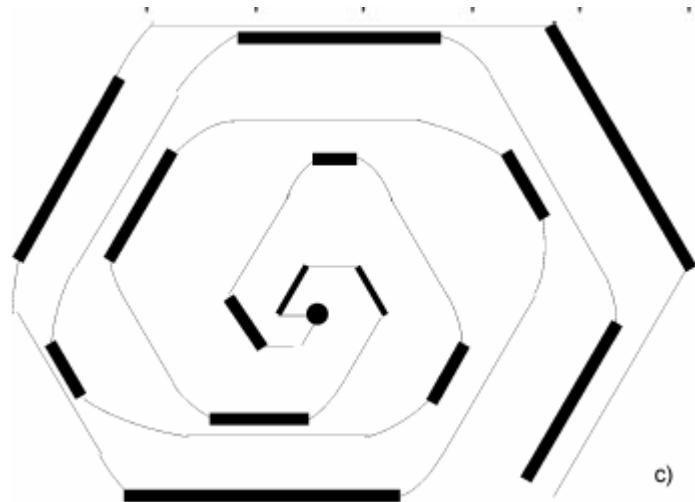
# Ga - double step structure



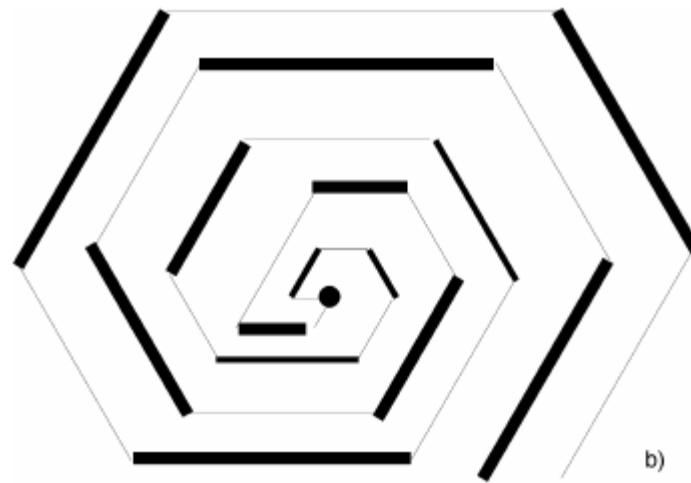
# Meandering



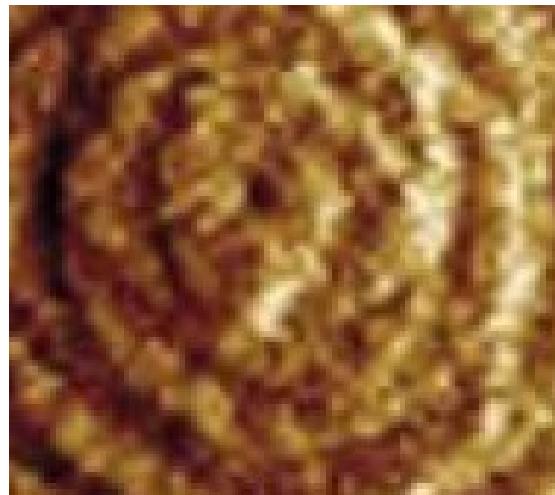
# Step evolution



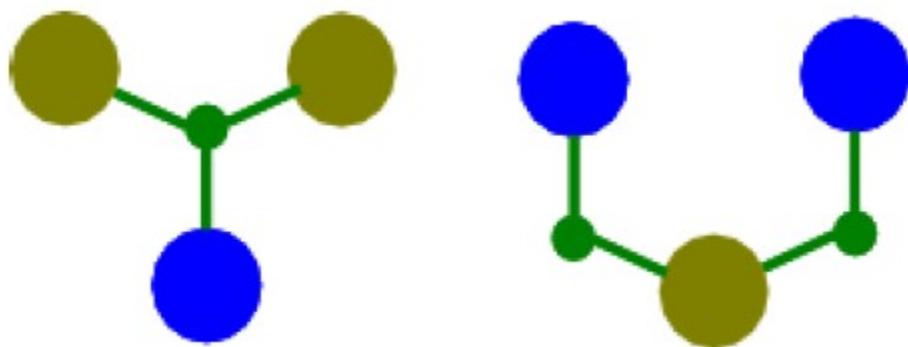
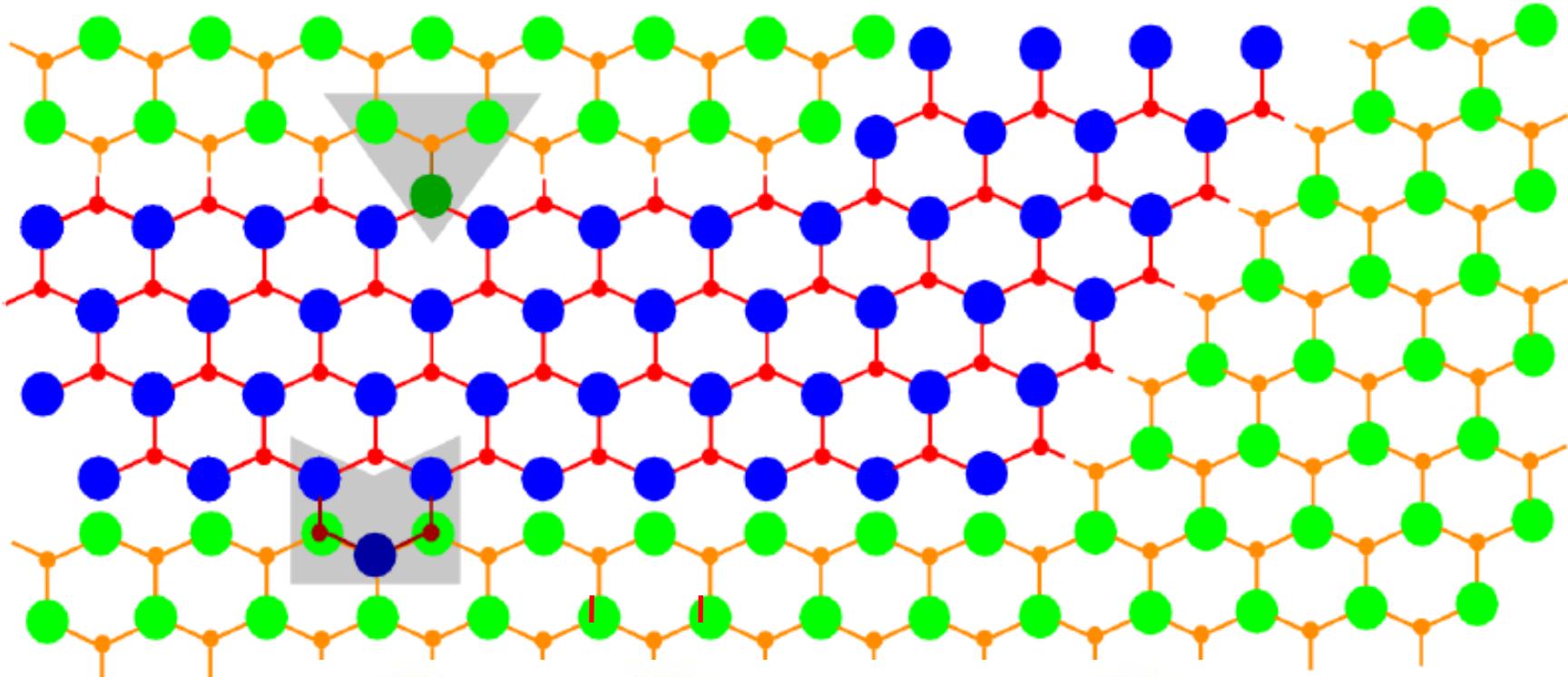
c)



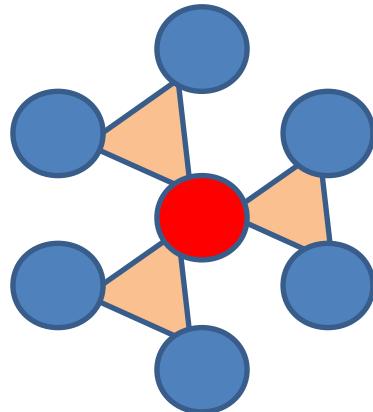
b)



# Interaction at steps



# Interaction

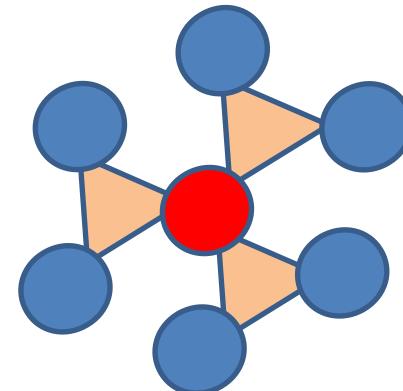


Even terrace

$$n_i = \begin{cases} 0 & \text{no neighbors} \\ \frac{1}{3}r & \text{two- body interactions} \\ 1 & \text{four-body interactions} \end{cases}$$

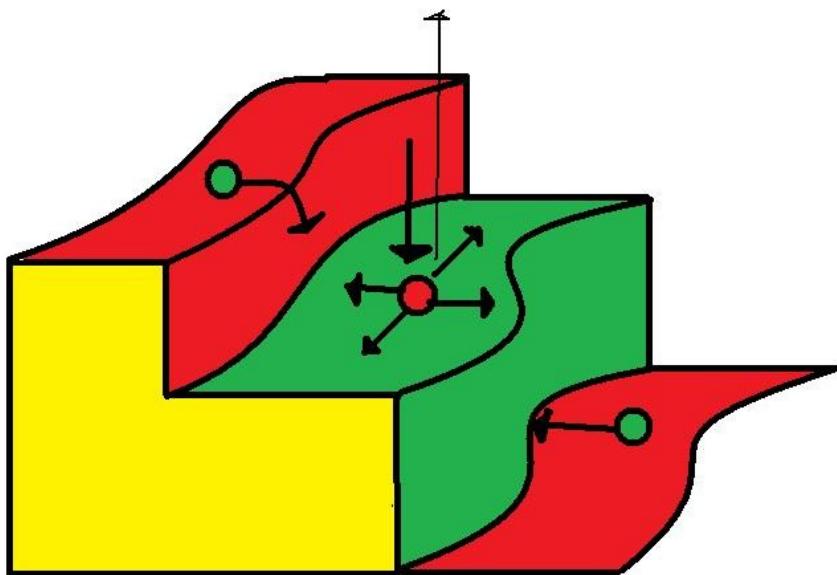
$$E(J) = J \sum_{i=1}^4 n_i$$

For  $r_o = 1$  steps are identical



Odd terrace

# Model of crystal growth



Terrace adsorption

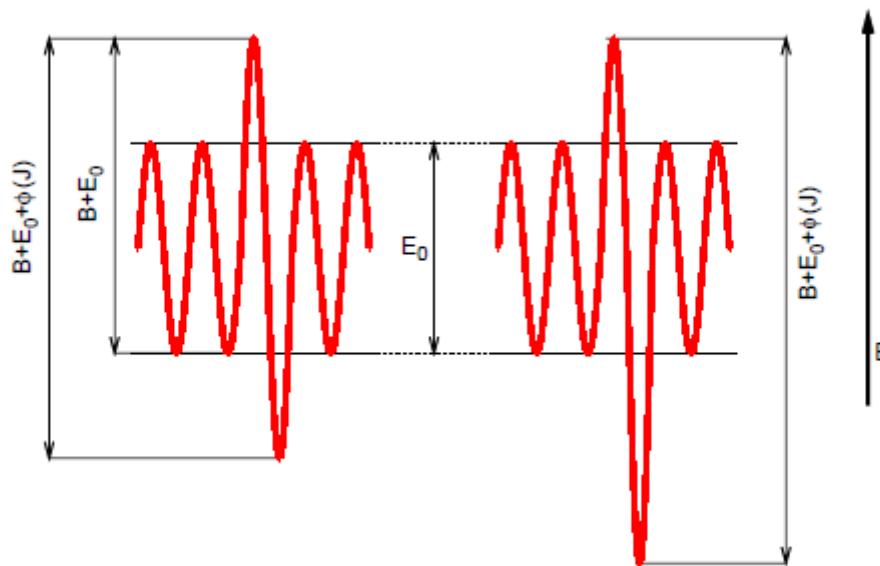
Surface diffusion

Step adsorption

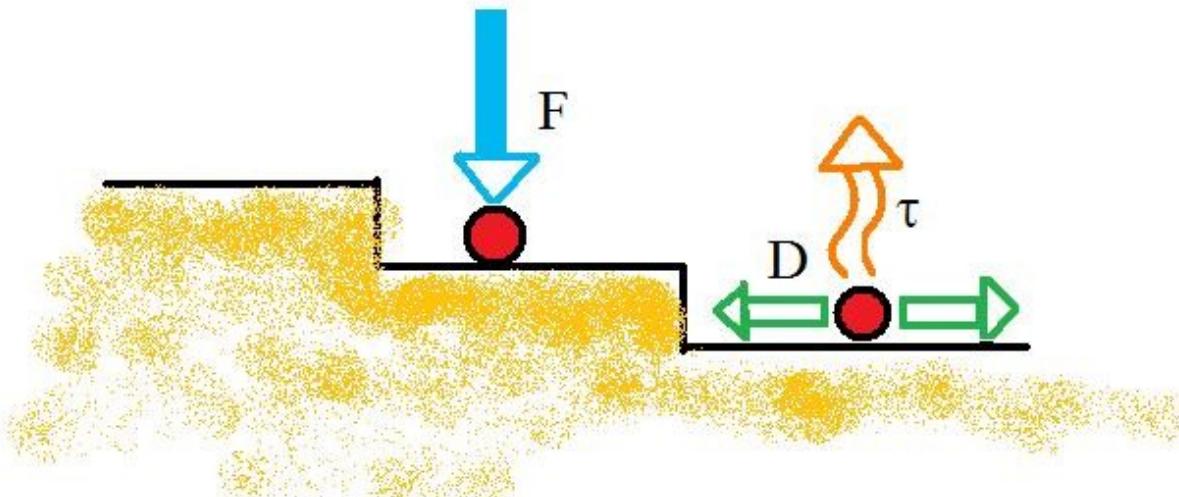
Jump step up and step down  
– Schwoebel barrier

External particle flux

# Potential at steps



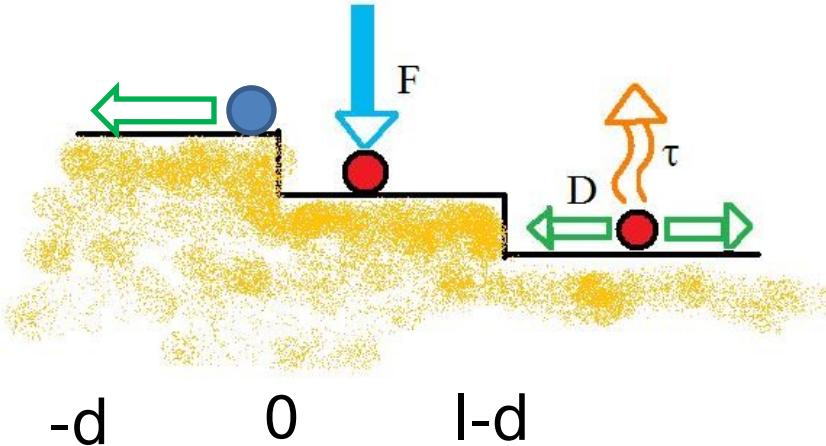
# Surface growth Burton-Carbera-Franck analysis



$$D\Delta\rho + F - \frac{1}{\tau}\rho = \frac{d}{dt}\rho$$

# Analytical model 1D parallel straight steps

$$D \frac{d^2}{(dz)^2} \rho + F - \frac{\rho}{\tau} + V \frac{d}{dz} \rho = 0$$



$$\begin{aligned} D \frac{d\rho}{dz} |_{(-d)+} &= k_1(\rho - \rho^+_1) |_{(-d)+} \\ -D \frac{d\rho}{dz} |_{0-} &= \kappa_2(\rho - \rho^-_2) |_{0-} \\ D \frac{d\rho}{dz} |_{0+} &= k_2(\rho - \rho^+_2) |_{0+} \\ -D \frac{d\rho}{dz} |_{(l-d)-} &= \kappa_1(\rho - \rho^-_1) |_{(l-d)-} \end{aligned}$$

$$V = D \frac{d\rho}{dz} |_{0+} + D \frac{d\rho}{dz} |_{0-} = D \frac{d\rho}{dz} |_{(-d)+} + D \frac{d\rho}{dz} |_{(l-d)-}$$

# Solution

$$\rho(z) = F\tau - A \cosh(\lambda z) - B \sinh(\lambda z)$$

$$\lambda = \sqrt{\frac{1}{D\tau}}$$

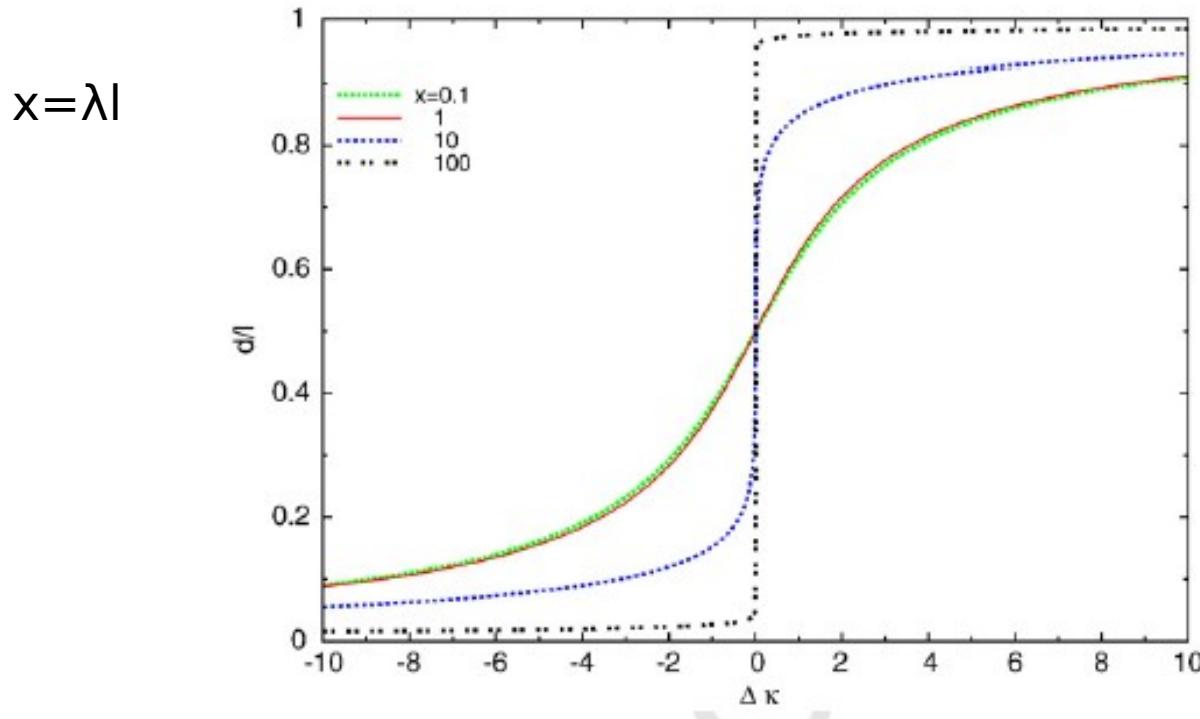
Pair of steps  $d$  and  $l-d$ . Width  $d$  is given by:

$$\begin{aligned} \frac{k_1 + \kappa_2}{k_1 - \kappa_2} \coth(\lambda d) - \frac{k_2 + \kappa_1}{k_2 - \kappa_1} \coth[\lambda(l - d)] &= \\ \frac{\kappa_1 k_2 + \lambda^2 D^2}{\lambda D(k_2 - \kappa_1)} - \frac{\kappa_2 k_1 + \lambda^2 D^2}{\lambda D(k_1 - \kappa_2)} \end{aligned}$$

for:  $(k_1 - \kappa_2)(k_2 - \kappa_1) > 0$

else:  $d=0$  double step structure

# Relative terrace width



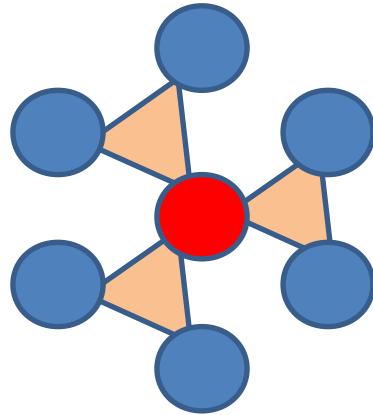
For high Schwoebel barrier

$$\coth(\lambda a) - \coth(\lambda(l-a)) = \frac{1}{\tau\lambda} \left( \frac{1}{\kappa_2} - \frac{1}{\kappa_1} \right)$$

$$\Delta\kappa = \frac{1}{\kappa_2} - \frac{1}{\kappa_1}$$

# Monte Carlo simulation

## 2D+1

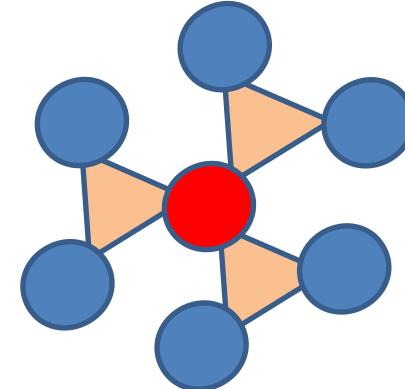


$$n_i = \begin{cases} 0 & \text{no neighbors} \\ \frac{1}{3}r & \text{two- body interactions} \\ 1 & \text{four-body interactions} \end{cases}$$

Even terrace

$$E(J) = J \sum_{i=1}^4 n_i$$

For  $r_o = 1$  steps are identical



Odd terrace

# Particle kinetics

Diffusion

$$D = v_d e^{-\beta(E(J) - E'(J))} \quad \begin{cases} \text{for } E(J) - E'(J) > 0 \\ \text{otherwise} \end{cases}$$

Adsorption +  $\beta = 1/(k_B T)$

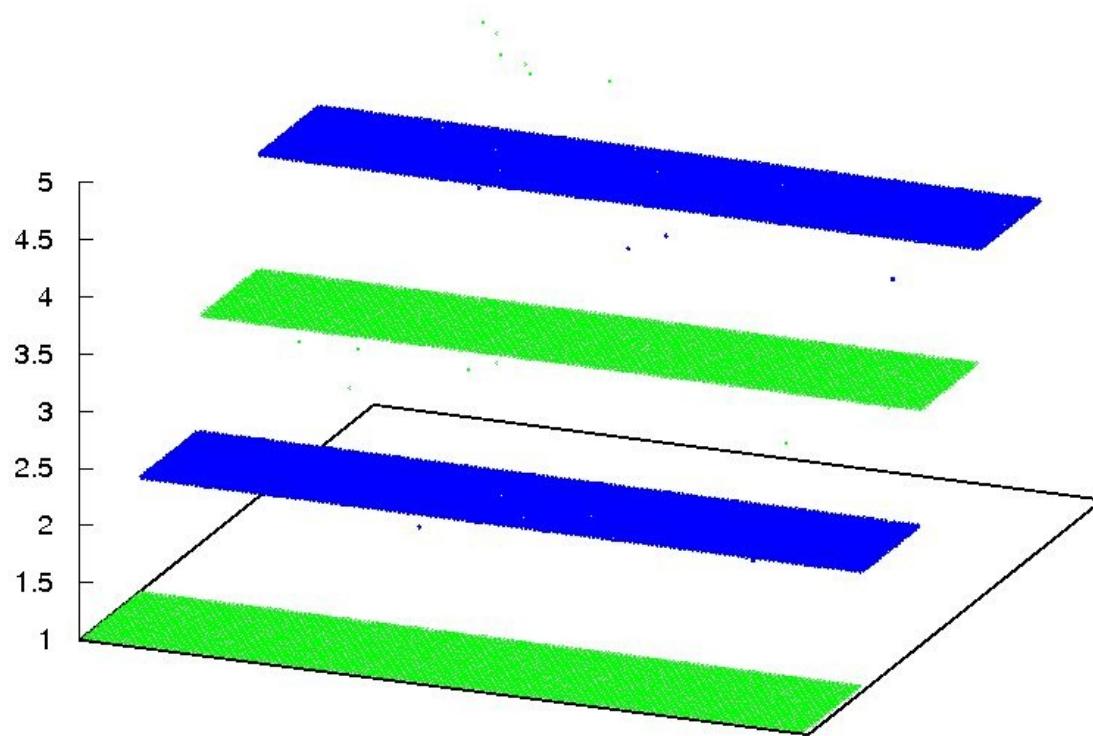
desorption  
 $F = v_a e^{-\beta \mu} = \tau^{-1}$

Jumps step down and step up

$$P_g = D e^{-\beta b_g}$$

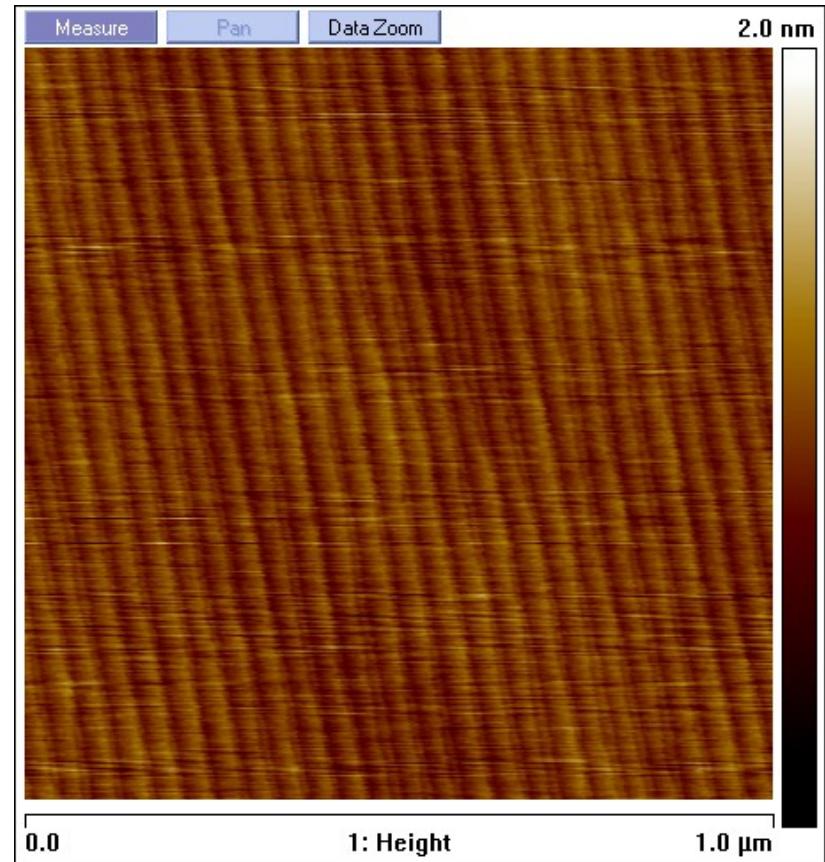
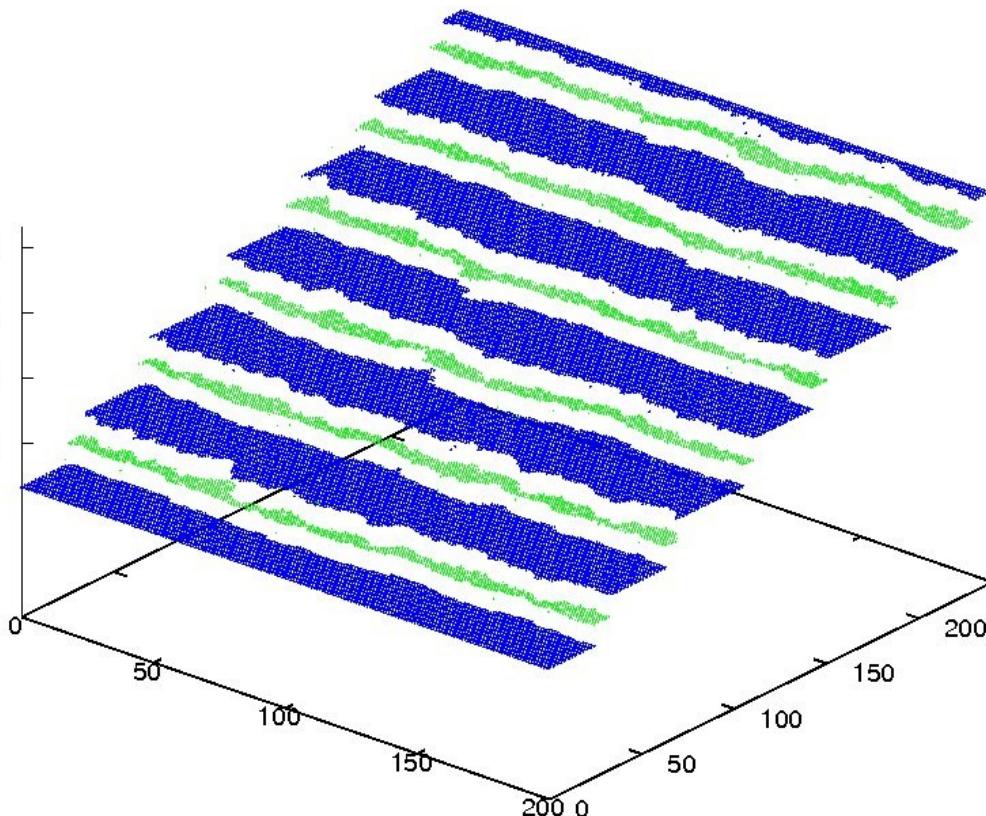
$$P_d = D e^{-\beta b_d}$$

# Initial configuration

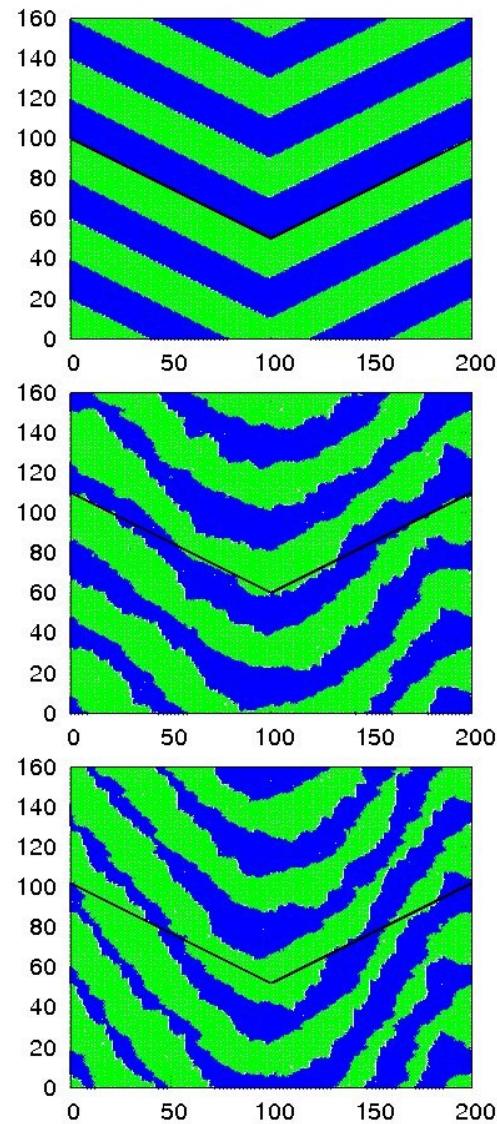


# Narrow terraces,high temperatures

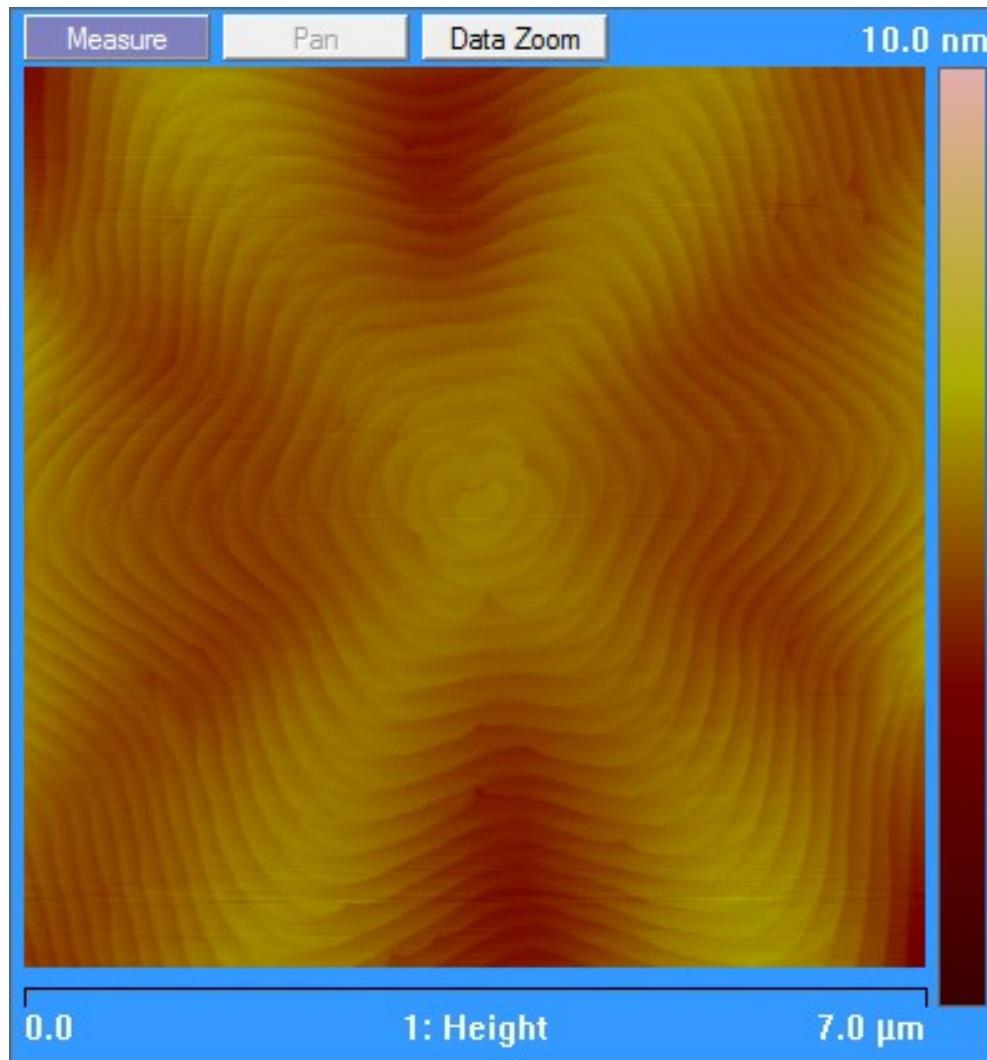
$r=0.4$ ,  $\beta J=5$  ,  $\beta\mu=15$ ,  $\beta b=0$ ,  
[0110]



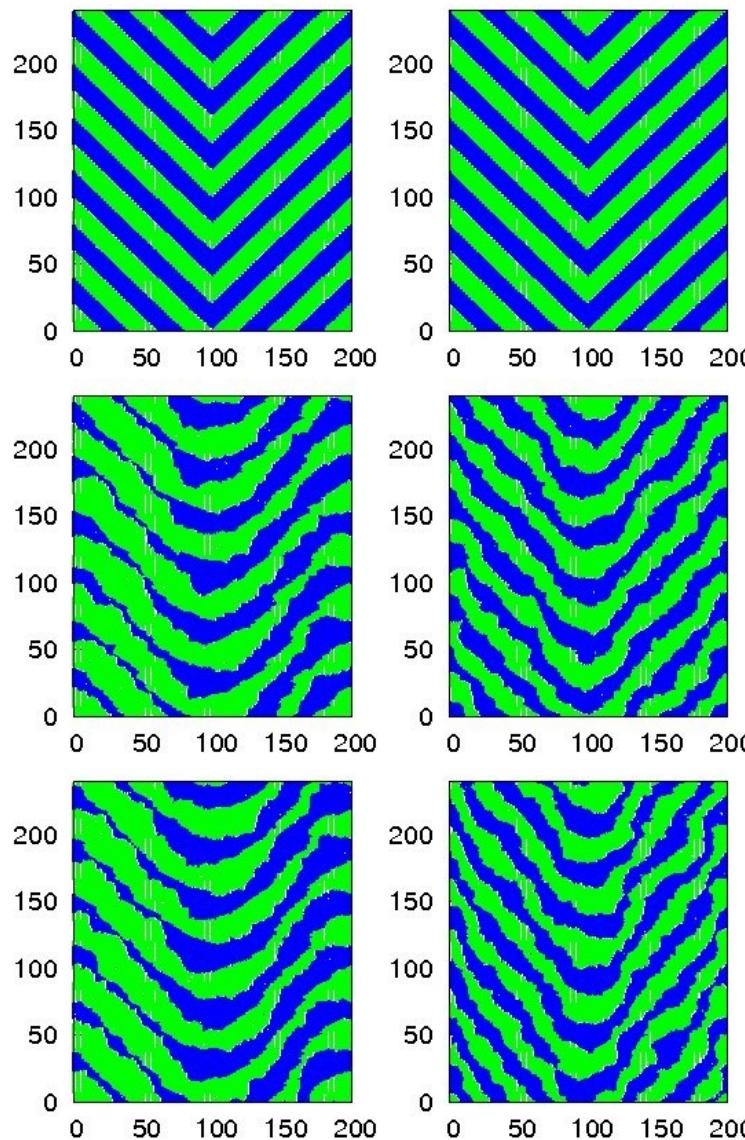
Marta Sawicka, Anna Feduniewicz-Żmuda, Marcin Siekacz, Henryk Turski,  
Czesław Skierbiszewski  
„Unipress” Institute of High Pressure Physics PAS, Poland



$r=0.4$ ,  $\beta J=5$ ,  $\beta\mu=15$ ,  $\beta b=0$ , [0110],  
[0101]

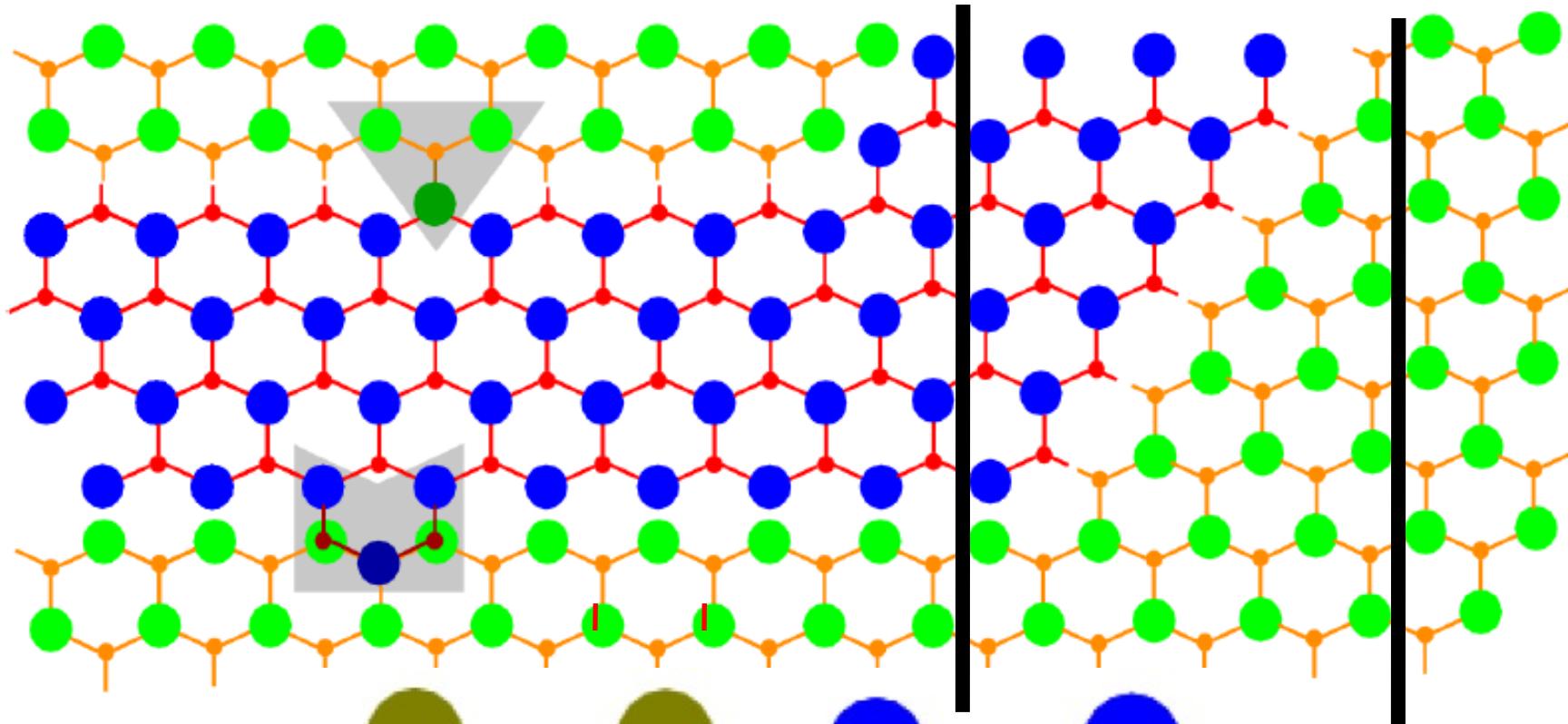


Robert Czernecki, Michał Leszczyński  
UNIPRESS, Institute of High Pressure Physics PAS, Poland



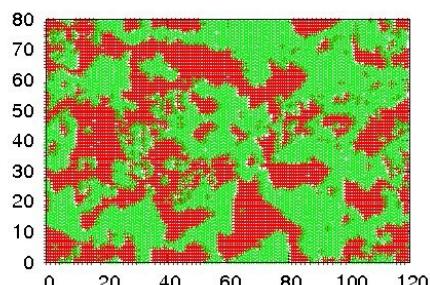
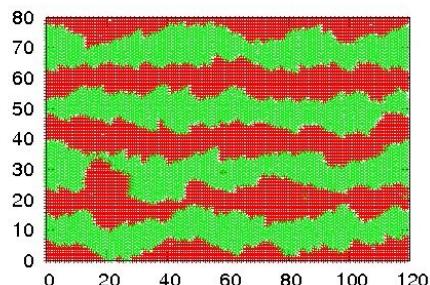
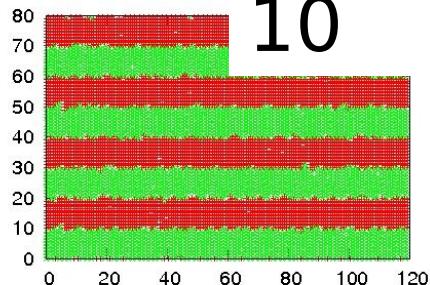
$r=0$ ,  $\beta^4 J=5$ ,  $\beta\mu=15$ ,  $\beta b=0$ ,  $20^\circ = 1$ ,  
[0110], [0101]

# Step [1120]

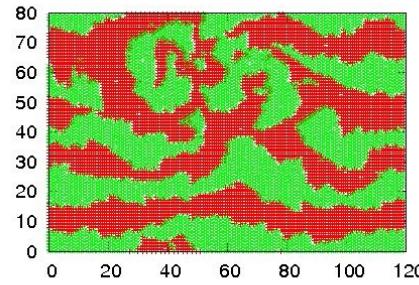
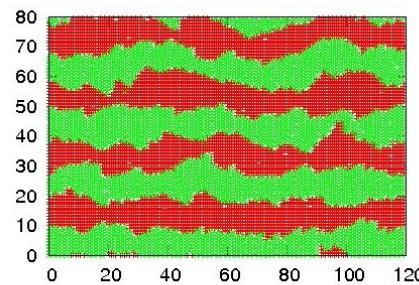
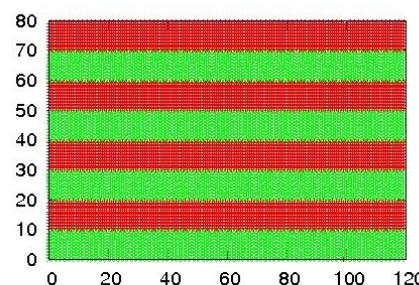


# Vertical cut

$r=0.4$     $\beta J=5,$     $d=$

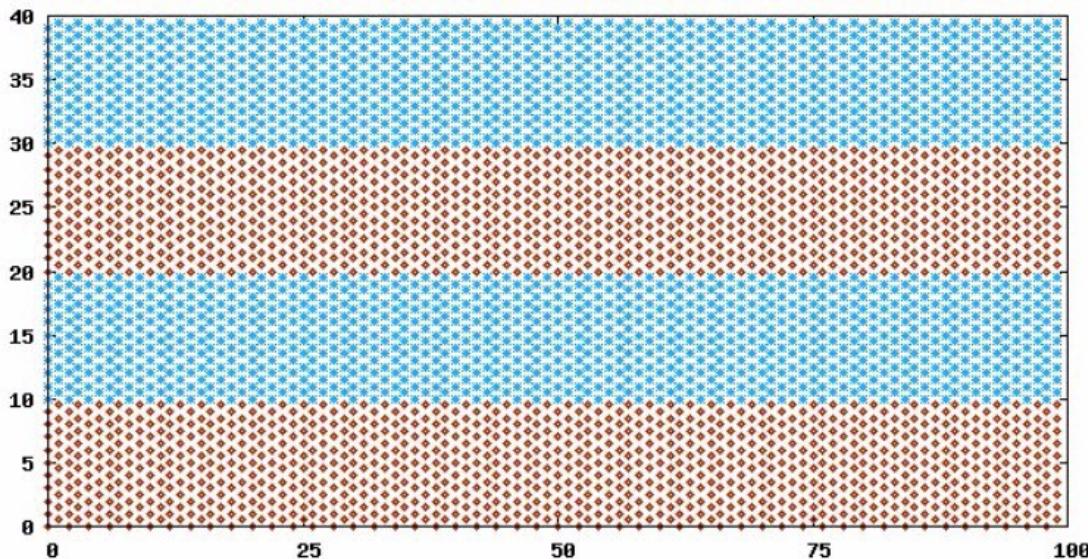


$b=1.5$



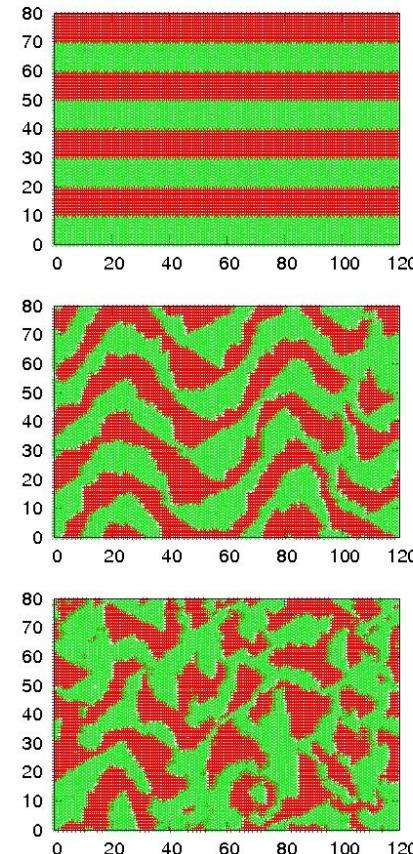
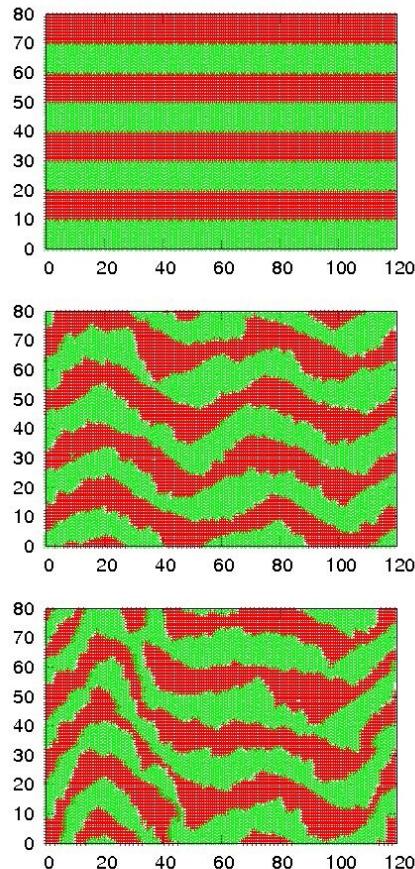
$b=1.05$

# Lower temperature



$r=0.4$ ,  $\beta J=5.8$  ,  $\beta\mu=15$ ,  $\beta b=0$ ,  
[1120]

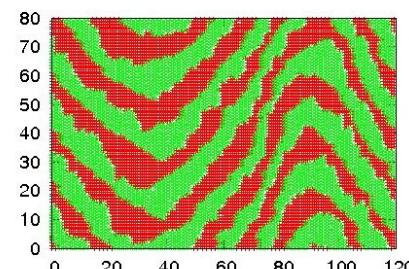
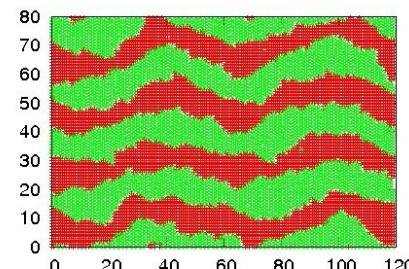
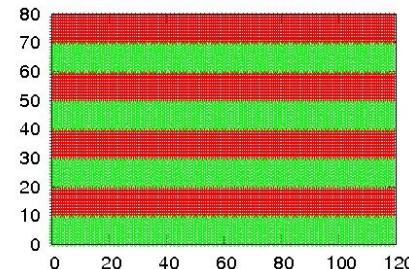
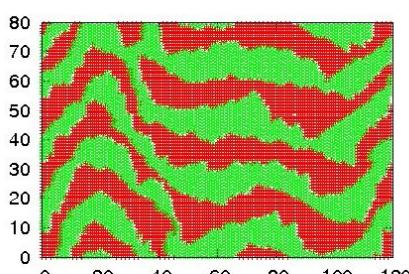
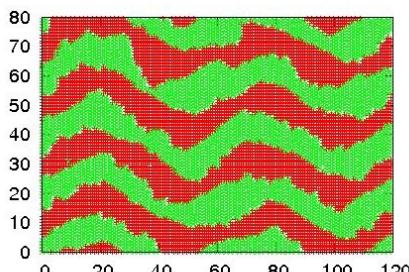
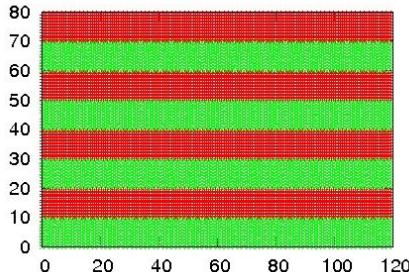
# Lower temperatures



$r=0.4, \beta J=6, \beta\mu=15, \beta b=0.7,$   
[1120]

$r=0.4, \beta J=6.5, \beta\mu=15, \beta b=0.7,$   
[1120]

# Low Schwoebel barrier

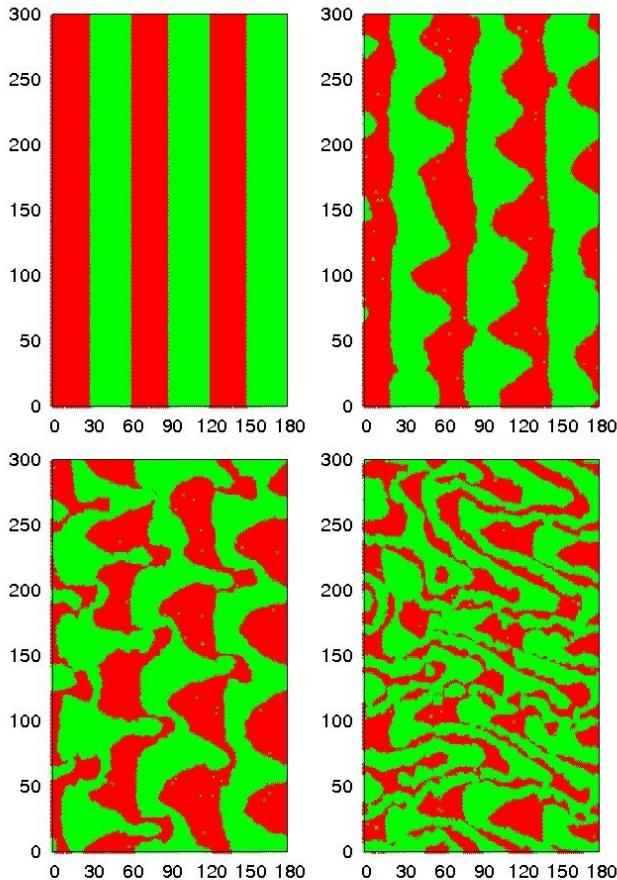


$r=0.4$ ,  $\beta J=6$ ,  $\beta\mu=15$ ,  $\beta b=0.7$ ,  
[1120]

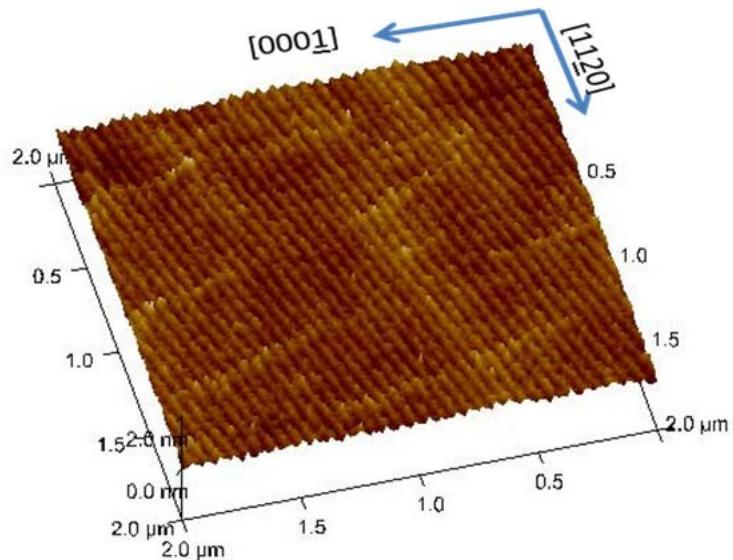
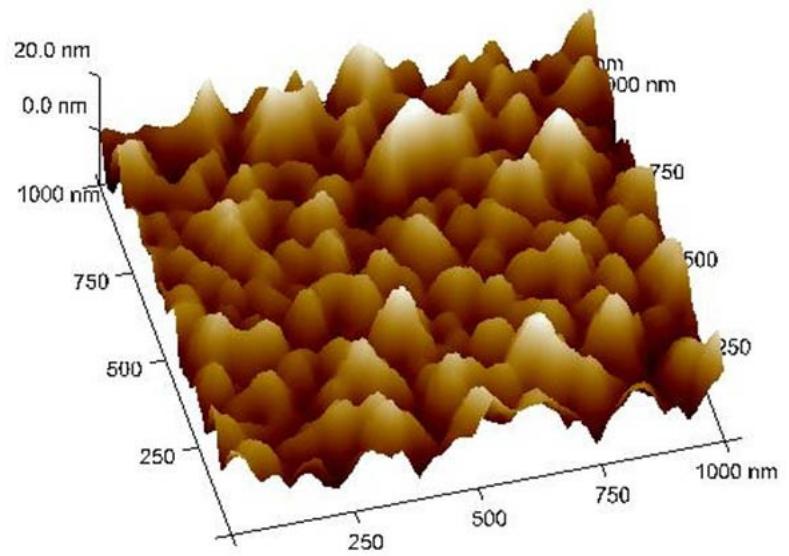
$r=0.4$ ,  $\beta J=6$ ,  $\beta\mu=15$ ,  $\beta b=0.$ ,  
[1120]

# Wider steps, lower temperatures, Schwoebel

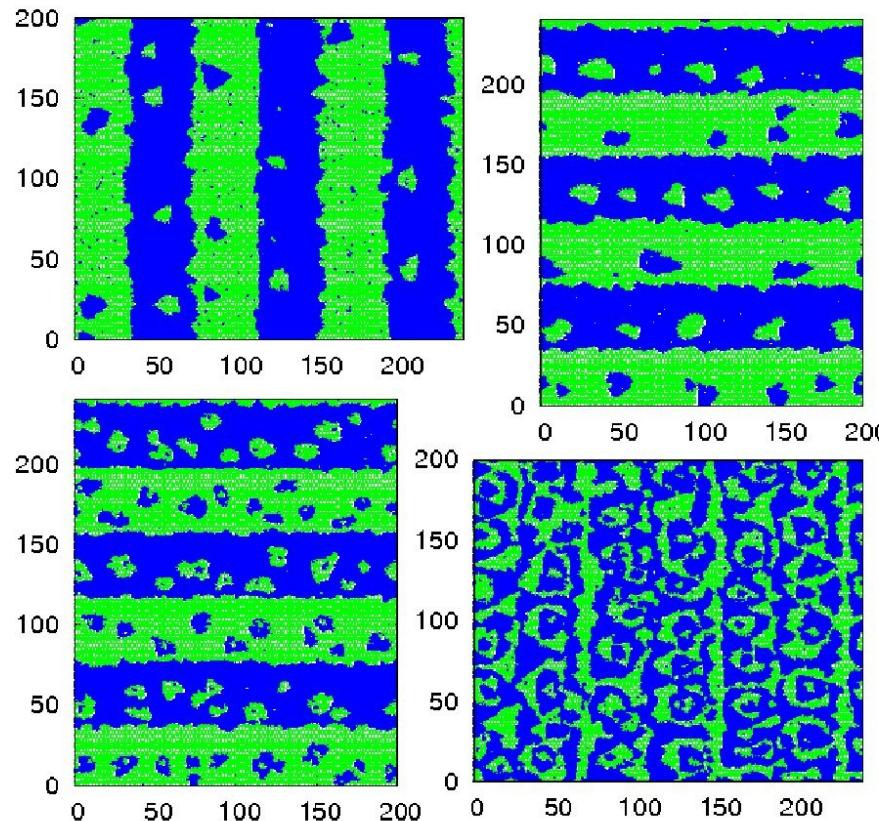
b = 0.5, r = 0.4



$r=0.4$ ,  $\beta J=6$ ,  $\beta\mu=16$ ,  $\beta b=0.5$ ,  
[0110]

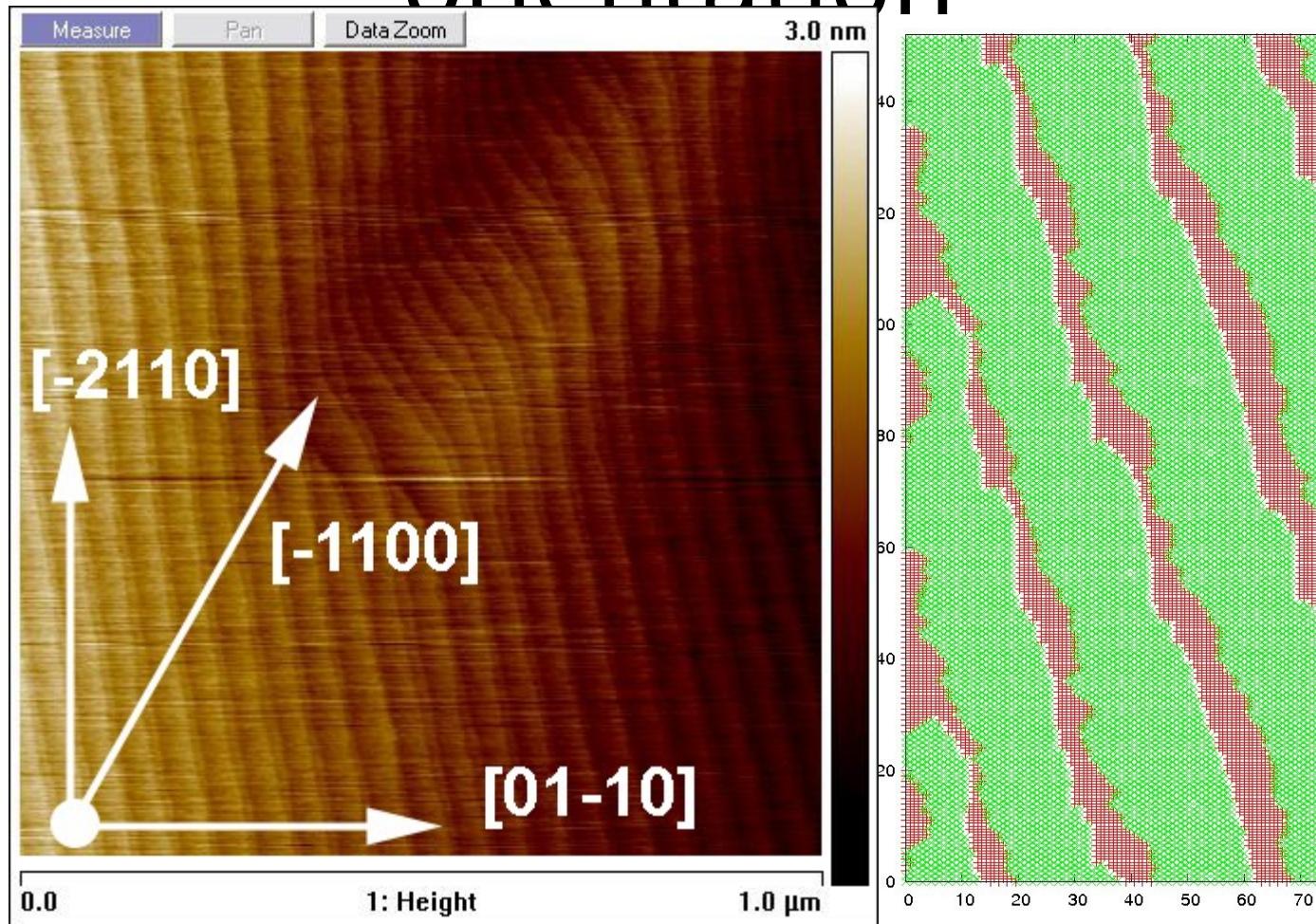


# Too large particle flux



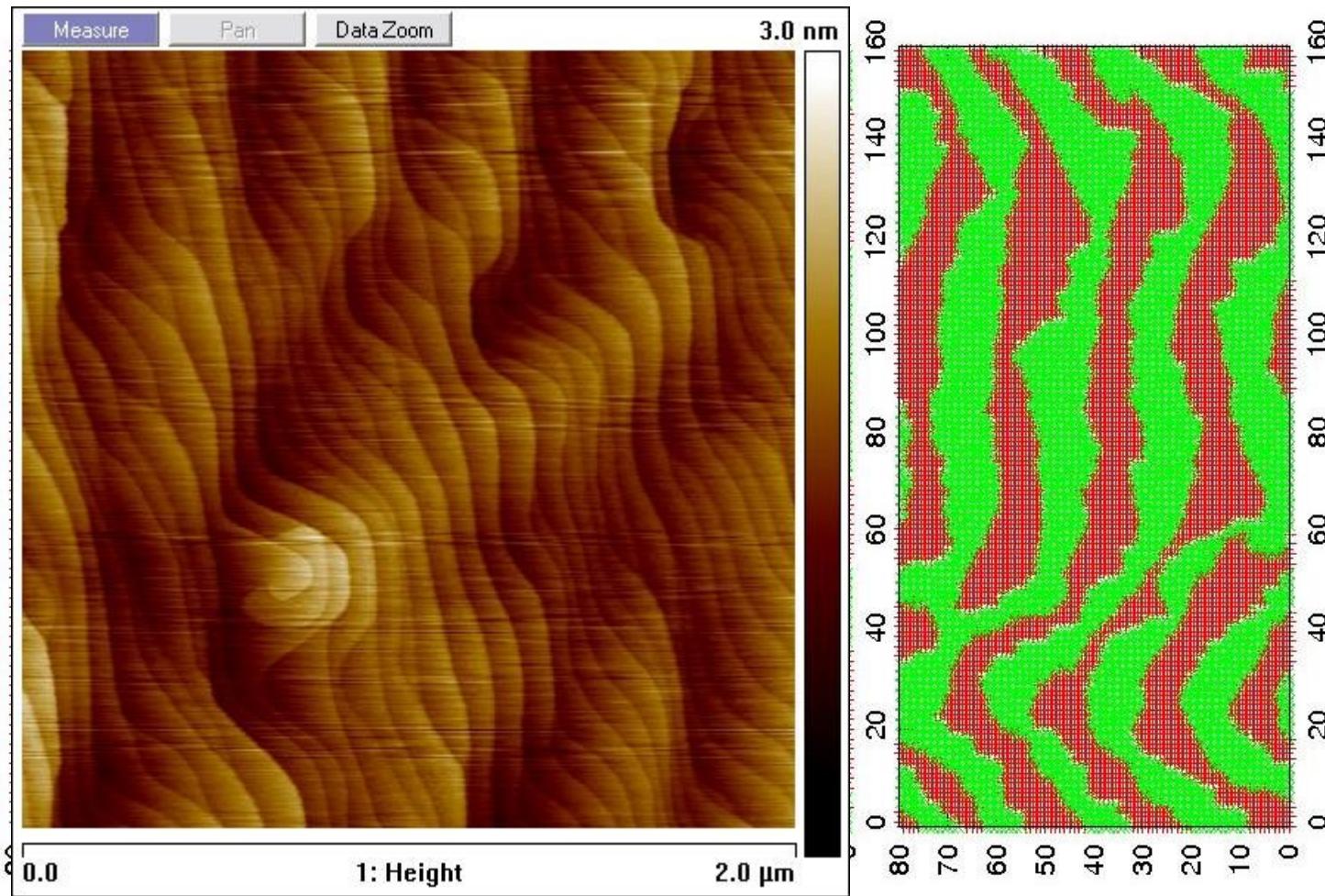
$r=0.2$ ,  $\beta J=5$  ,  $\beta\mu=13$ ,  $\beta b=0$ ,  
[0110]

# Dependence on the step orientation



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# [1210] orientation



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# Model parameters

Step asymmetry and temperature

$$r \qquad \beta J = J / (k_B T)$$

External particle flux

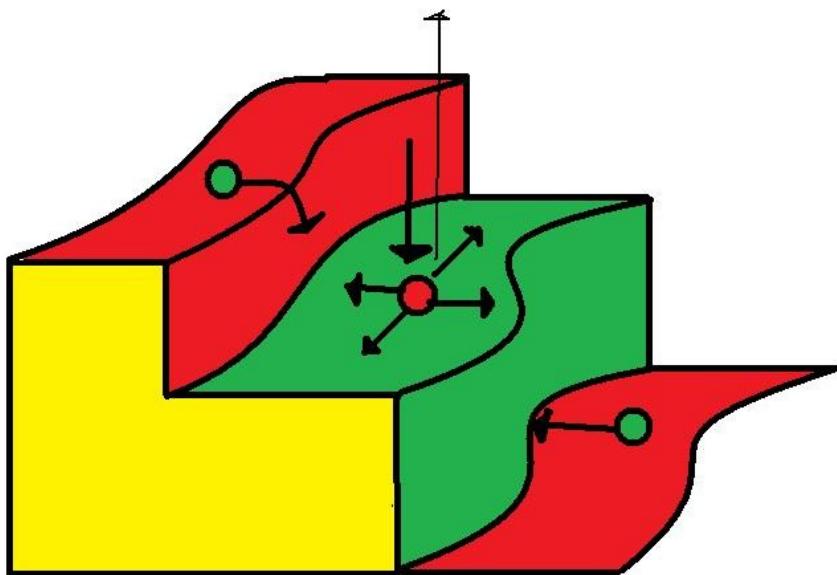
$$F = v_a e^{-\beta u} = \tau^{-1}$$

Schwoebel barrier

$$P_g = D e^{-\beta b_g}$$

$$P_d = D e^{-\beta b_d}$$

# Control parameters



Terrace width

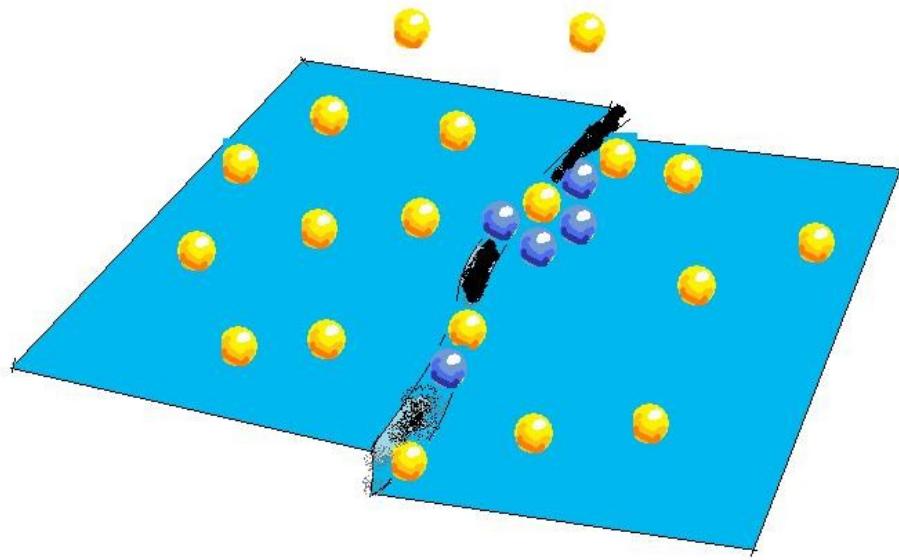
Orientation of steps

Temperature

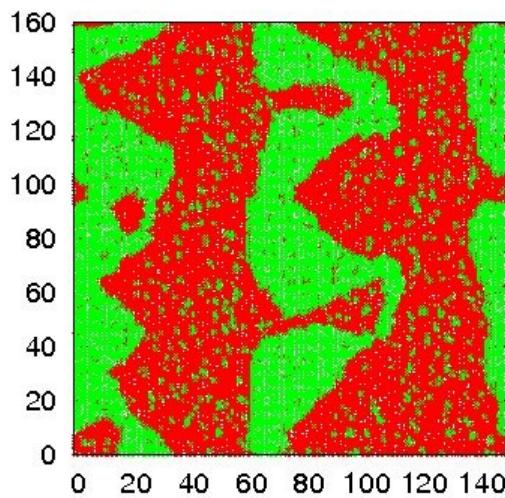
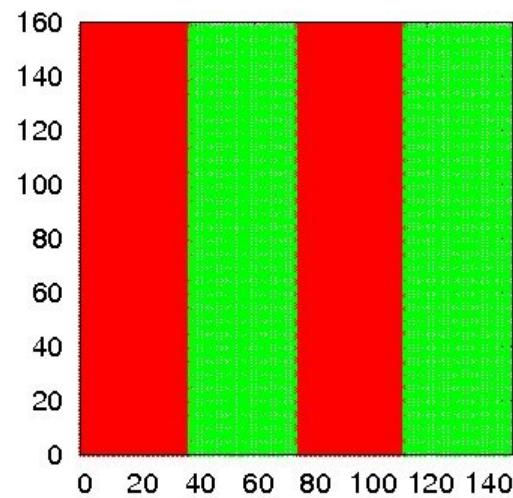
External particle flux

Other particles i.e.: Indium

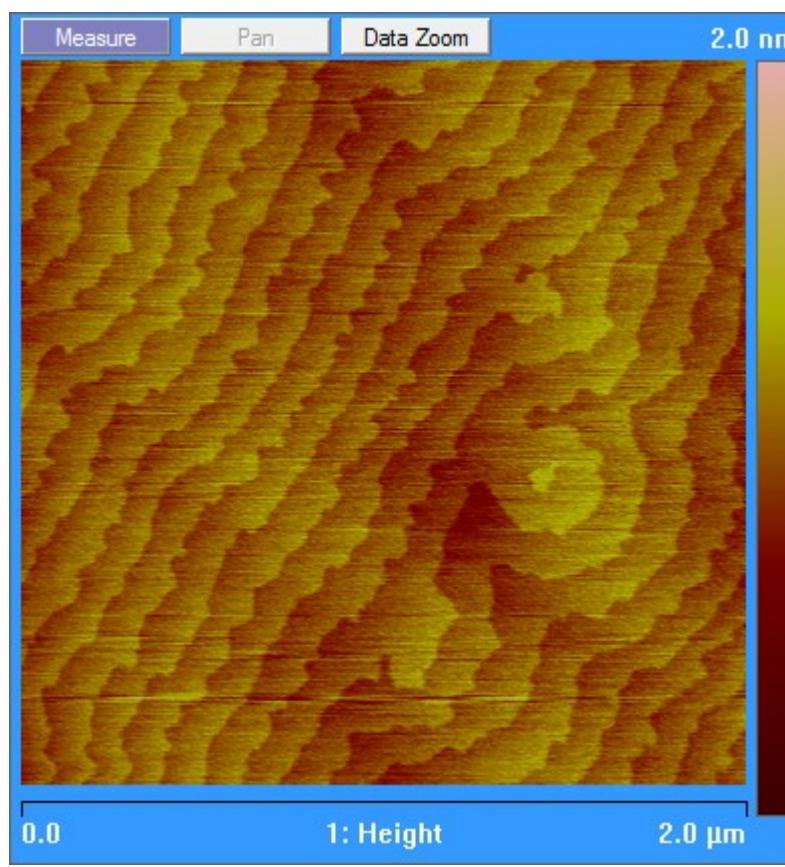
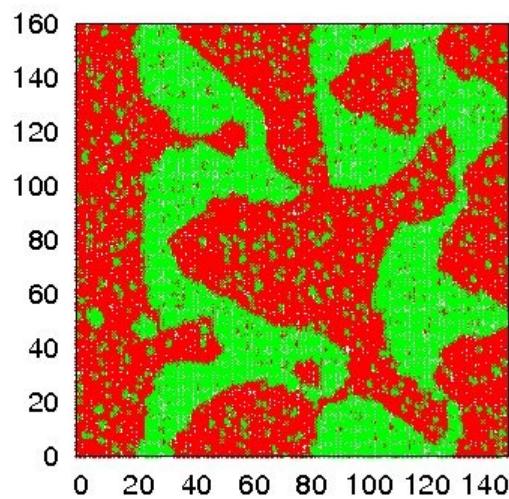
# GaN+Indium



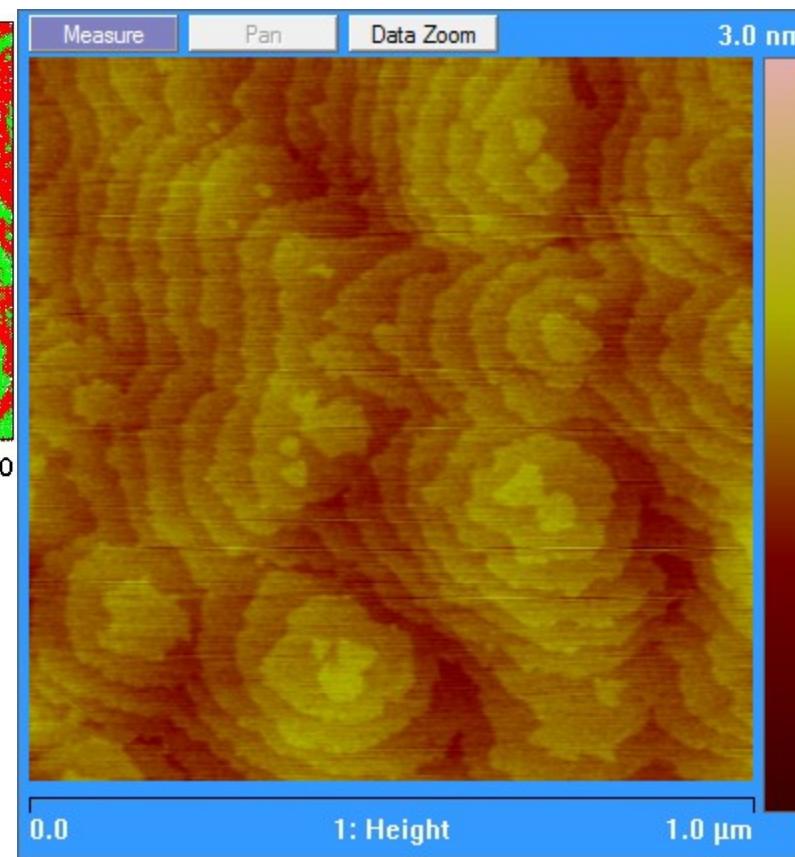
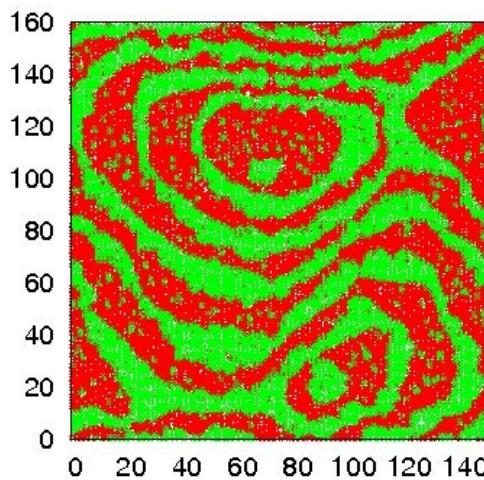
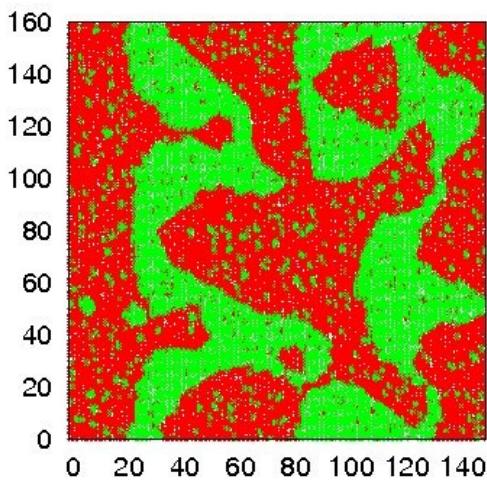
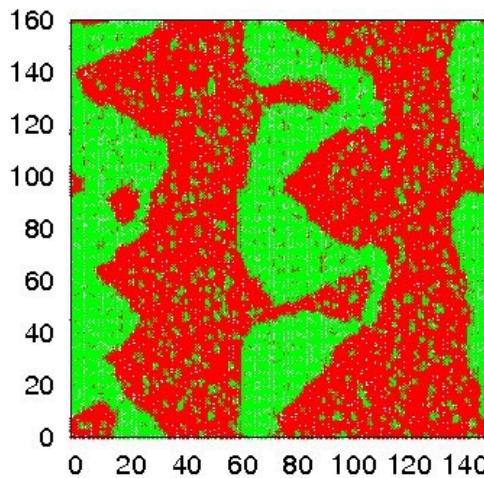
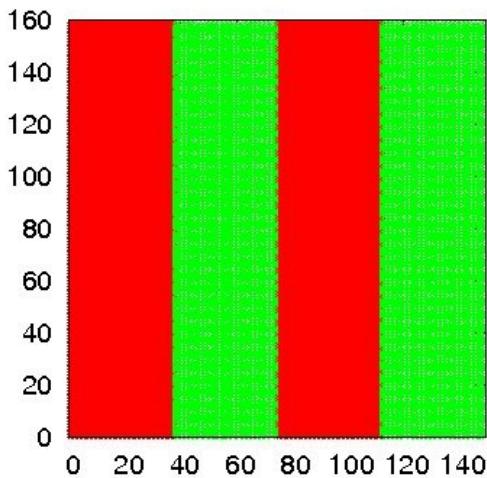
One more component in the model



ndium



# Indium



# Summary

1. Three regimes of step flow during growth on GaN(0001) surface are observed:

- low misorientation - very large terrace width - single straight step flow
- medium misorientation - medium terrace width - step meandering
- large misorientation - small terrace width - double and multiple straight step flow

1. Depending on the orientation of the step - two different crystallographic consecutive step structure can be created on GaN(0001) surface:

2. Rotation by 60 arc deg exchanges these two steps types.

3. Monte Carlo simulations describes:

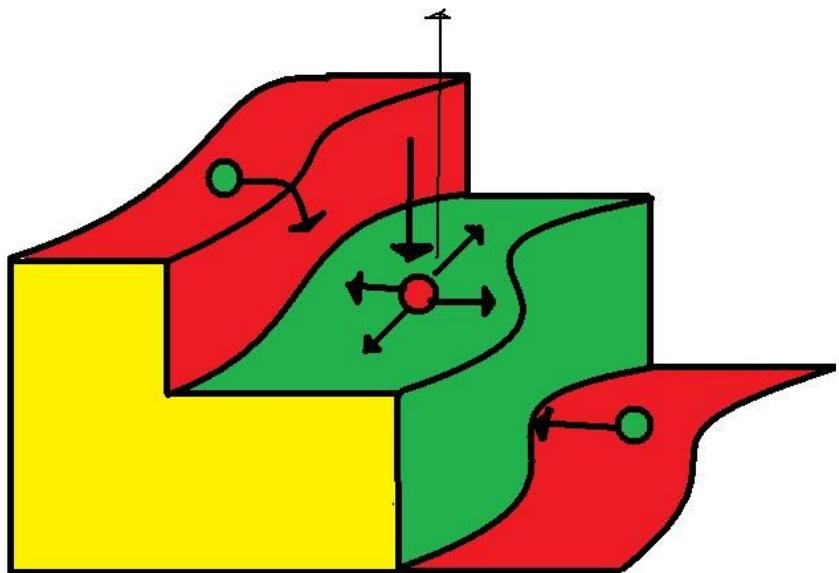
- 2-d nucleation controlled growth mode for large supersaturations
- step flow mode for smaller supersaturations.

1. Monte Carlo simulations recovers step meandering and transition to double step flow modes.

2. Step meandering emerges in the result of diffusive interaction between steps and step anisotropy

# Analytical model 1D - parallel straight steps

$$D \frac{d^2}{(dz)^2} \rho + F - \frac{\rho}{\tau} + V \frac{d}{dz} \rho = 0$$



$$D \frac{d\rho}{dz} |_{(-d)+} = k_1(\rho - \rho^+_{-1}) |_{(-d)+}$$

$$-D \frac{d\rho}{dz} |_{0-} = \kappa_2(\rho - \rho^-_{-2}) |_{0-}$$

$$D \frac{d\rho}{dz} |_{0+} = k_2(\rho - \rho^+_{+2}) |_{0+}$$

$$-D \frac{d\rho}{dz} |_{(l-d)-} = \kappa_1(\rho - \rho^-_{-1}) |_{(l-d)-}$$

$$V = D \frac{d\rho}{dz} |_{0+} + D \frac{d\rho}{dz} |_{0-} = D \frac{d\rho}{dz} |_{(-d)+} + D \frac{d\rho}{dz} |_{(l-d)-}$$

# Stability analysis of steps

When parallel steps start to meander?

$$z_i(x) = z_i^0 + \epsilon_i \sin(kx + \omega t)$$

$$\begin{aligned}\rho(x, z, t) &= A_0 \sinh(\lambda z(x, t)) + B_0 \sinh(\lambda z(x, t)) \\ &\quad + \epsilon [A_1 \sinh(\Lambda z) + B_1 \sinh(\Lambda z)] \sin(kx + \omega t)\end{aligned}$$

$$\rho^\pm_i = \rho^\pm_{i0} - \Gamma \frac{z_{xx}}{(\sqrt{1 + z_x^2})^3}$$

$$V = \frac{V_0 + \dot{z}}{\sqrt{1 + z_x^2}}$$

$$\omega(k_c) = 0 \quad \frac{\partial \omega}{\partial k} \Big|_{k=k_c} = 0$$

# Solution

Steps destabilize when

$$\frac{\lambda\Gamma}{F\tau} \left[ \coth(\lambda d) \frac{k_1 + \kappa_2}{k_1 - \kappa_2} + \frac{(D\lambda)^2 + k_1\kappa_2}{D\lambda(k_1 - \kappa_2)} \right] < \frac{1}{2},$$

Double steps destabilize for

$$\frac{\lambda\Gamma}{F\tau} \left[ \coth(\lambda l) \frac{k + \kappa}{k - \kappa} + \frac{(D\lambda)^2 + k\kappa}{D\lambda(k - \kappa)} \right] < \frac{1}{2}$$

$$(\lambda\Gamma)/(F\tau) < 1/2$$

# Step dynamics

