

# EDGE RESONANCE AT VIBRATION AND ELASTIC WAVES EXCITATION IN THREE-DIMENSIONAL ANISOTROPIC BODIES OF THE HEXAGONAL SYSTEM

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**Summary** The results of edge resonance effects theoretical research for the case of axisymmetric vibrations in transversally-anisotropic solid plates and rings and the case of waves excitation in transversally-anisotropic semi-layer and anisotropic semi-cylinder are presented. Numerically-analytical method of rows on base great number of travelling and edge standing normal waves was applied to studied problems. Effects of frequency spectrums and edge resonance shapes transformation are described.

Edge resonances by transversally anisotropic solids and rings axisymmetric vibrations and waves excitation in transversally anisotropic semi-layer and anisotropic semi-cylinder theoretical research results are presented. Numerically-analytical method on base great number of travelling and edge standing normal waves was applied to studied problems.

It was fined the special wave anisotropy rate parameter  $\Delta_m$  that defines a structure of travelling and edge standing waves dispersion spectrums (Fig. 1, Fig. 2) and edge resonance features in studied bodies. This parameter is determine by ratio  $\Delta_m = (1 - 4\alpha_1\delta_1) / \beta_1^2$ , where  $\alpha_1 = s_1^2\mu_2$ ,  $\delta_1 = s_1^2(\mu_1 + 1)$ ,  $\beta_1 = s_1^4 + \mu_2(\mu_1 + 1) - \mu_3^2$ ,  $s_1^2 = 2c_{44} / (c_{11} - c_{12})$ ,  $\mu_1 = (c_{11} + c_{12}) / (c_{11} - c_{12})$ ,  $\mu_2 = 2c_{33} / (c_{11} - c_{12})$ ,  $\mu_3 = 2(c_{13} + c_{44}) / (c_{11} - c_{12})$ ,  $c_{ij}$  - elasticity constants of hexagonal system anisotropic material.

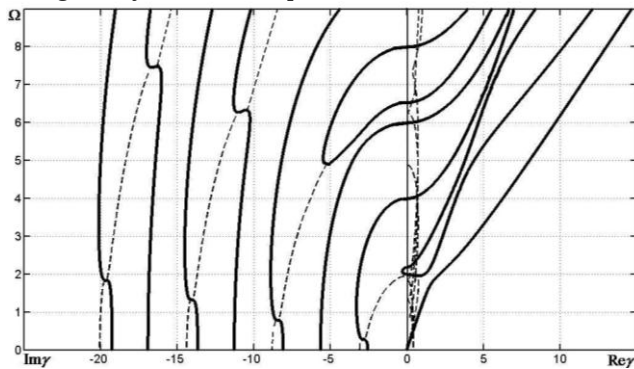


Fig. 1 Dispersion spectrum of Co crystal plate

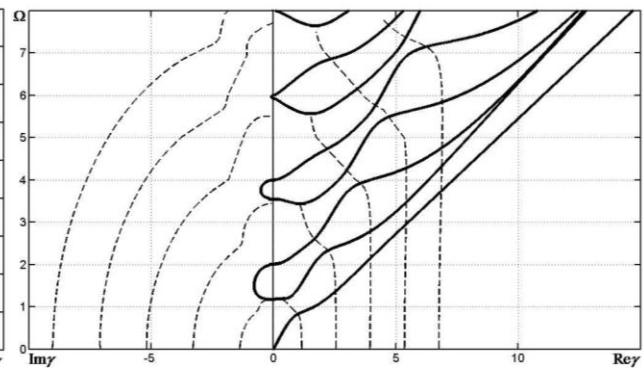


Fig. 2 Dispersion spectrum of Zn crystal plate

Amplitude-frequency and frequency-phase dependences for disk plates and rings dynamical characteristics was obtained and analyzed applied to some real ceramic and crystal materials with different values of generalized wave anisotropy parameter  $\Delta_m$ . Dependences of resonance frequencies from studied bodies' geometric characteristics are obtained. Theoretical method of edge resonance frequencies  $\Omega_e$  finding and vibration shapes on these frequencies building was developed. High match level of obtained by this method and presented in the paper [1] results for  $BaTiO_3$  piezoceramic solid plate was received.

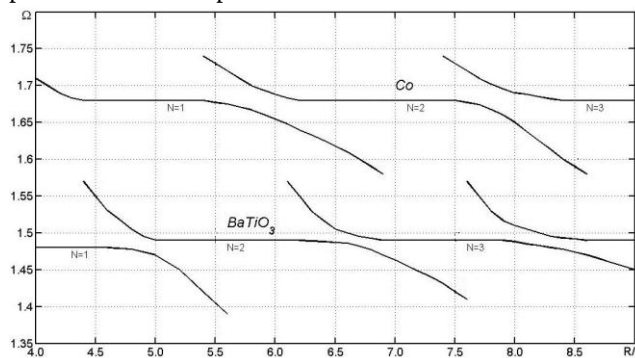


Fig. 3 Edge resonance spectrums for Co ( $\Delta_m = 0.64$ ) and  $BaTiO_3$  ( $\Delta_m = 0.023$ ) plates

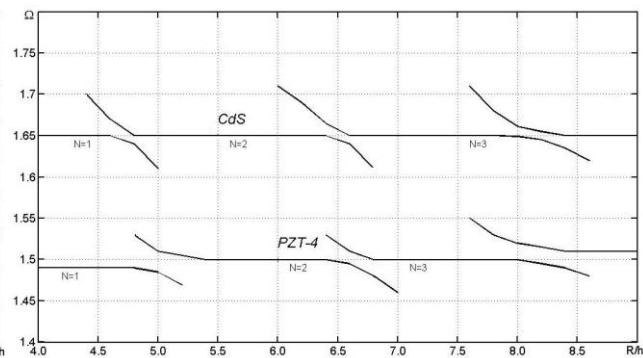


Fig. 4 Edge resonance spectrums for CdS ( $\Delta_m = 0.4$ ) and PZT-4 ( $\Delta_m = 0.055$ ) plates

The effect of edge resonance frequency  $\Omega_e$  growth for solid plates with positive growing by module parameter  $\Delta_m$  was established (Fig. 3, Fig. 4), in particular  $\Omega_e$  increase on 0.4% for  $BaTiO_3$  plates, on 1.15% for  $PZT-4$ , on 11.82% for  $CdS$ , on 13.24% for  $Co$  crystal. The effect of  $\Omega_e$  decrease for solid plates with negative growing by module parameter  $\Delta_m$  was established, in particular  $\Omega_e$  decrease on 1.01% for  $ZTP-19$  ceramic plates. The absence of edge resonance effect in concerned axisymmetric oscillations frequency range for solid plates with large-module negative  $\Delta_m$  was established, in particular for  $Cd$  and  $Zn$  crystals.

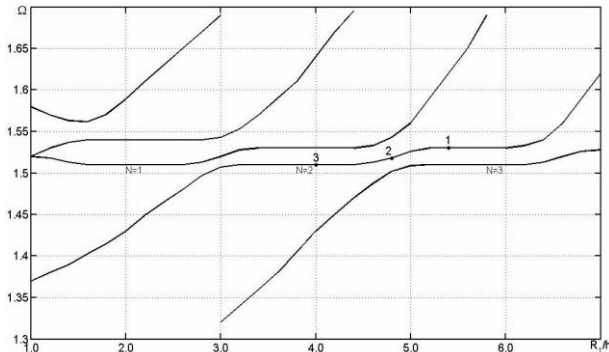
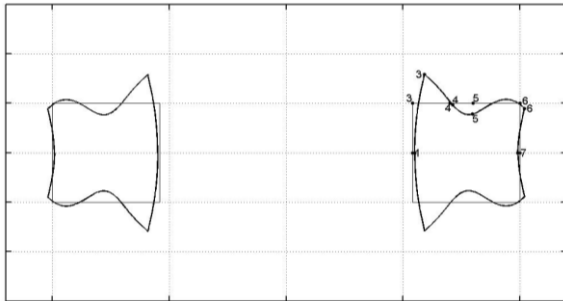
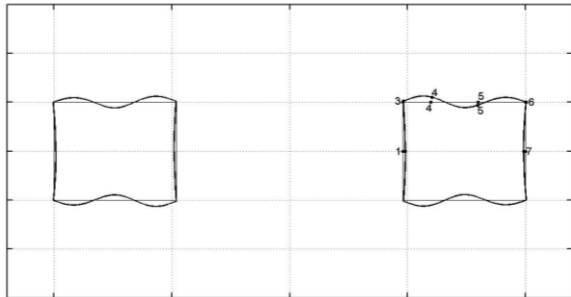


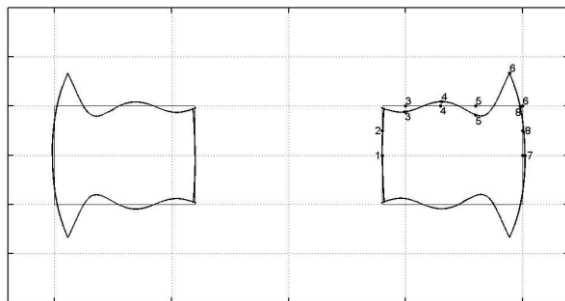
Fig. 5 Edge resonance spectrum for  $BaTiO_3$  ring



a) The shape in point 1 on fig. 5



b) The shape in point 2 on fig. 5



c) The shape in point 3 on fig. 5

Fig. 6 Vibration shapes for  $BaTiO_3$  ring.

It was showed that more contrast increase of edge standing waves excitation intensity on edge resonance frequencies is inherent for plates with small by module  $\Delta_m$  values. Frequency dependencies of edge standing waves excitation rates for large-module positive  $\Delta_m$  plates near  $\Omega_e$  have more monotonic character and the relational rate of lowest edge standing wave mode in this case is decreasing. In particular the mentioned rate for  $Co$  plate is nearly in 54 times less than for  $BaTiO_3$  solid plate.

The edge resonance effect also was researched in transversally-anisotropic rings. It was established that plateau-areas in the frequency spectrum have two-level structure conditionally on relations of rings geometrical and mechanical parameters. In particular (Fig. 5) for  $BaTiO_3$  ring the changing of resonance frequency value by jumping from the top mesa to the lower is going with the changing of edge resonance type from localized on the inside cylindrical surface (Fig. 6a) to the outside cylindrical surface localized (Fig. 6c). Oscillation localization on the frequency between mesa arrears is absent (Fig. 6b).

In regard to symmetrical waves excitation in transversally-anisotropic semi-layer the empirical regularity of edge resonance frequency  $\Omega_e$  increase that is characterized by growing positive parameter  $\Delta_m$  relatively to edge resonance frequency for isotopic semi-layer was obtained. In particular the mentioned growing is 0.7% for  $BaTiO_3$  semi-layer, 2.0% for  $PZT-4$  semi-layer, 12.1% for  $CdS$  and 14.9% for  $Co$  semi-layers. The edge resonance effect in transversally-anisotropic semi-layer with large-module negative  $\Delta_m$  value is not occurring in the mentioned frequency area, in particular for  $Cd$  and  $Zn$  semi-layers.

The physical law of edge resonance oscillations shapes near the transversally-anisotropic semi-layer border zone was researched. Vertical wave displacements levels in an angular point of semi-layer's section, that are defined mentioned oscillation intensity levels, are decreasing in line with increasing of positive semi-layer material characteristic  $\Delta_m$ .

The existence of edge resonance effects in transversally-anisotropic semi-cylinder by axisymmetric P-SV waves excitation is established. It was also ascertained that in the researched case of semi-cylinder material isotropy axis orientation a regular dependence between edge resonance frequency values and general wave anisotropy parameter  $\Delta_m$  is absent.

## References

- [1] Shaw E.A.G. On the resonant vibration of thin barium titanate disks / E.A.G. Shaw // J. Acoust. Soc. Amer. – 1956. – V. 20, № 1. – P. 38-50.