

ON IMPACT INTERACTIONS OF THE DAMAGED MEDIUM WITH THE FLOW OF THE CAVITATING LIQUID

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Summary The detailed analysis of local processes impact interaction between deformable damageable medium and cavitating liquid flow, caused erosion fracture is accomplished. This analysis is founded on results of researching local hydrodynamic flows in two- phases liquids, which have obtained authors recently. The complex phenomena in similar mediums require using separate processes method for investigation.

Problem review

The single steam bubble fracture leads to appearance swirl and cumulative stream of liquid. [1]. It was theoretically established and experimentally proved that limited value of speed wall single water steam ($\rho_g^0 = 0.562 \text{ kg/m}^3$) bubble with size $R_0 = 0.13410\text{-}3 \text{ m}$ under normal state $P_g = 0.1 \text{ MPa}$, $T_g = 373 \text{ K}$ under compressible triangular form pressure wave with amplitude $P_b = 30 \text{ MPa}$ and duration $t_b = 0.26 \text{ e-}03 \text{ s}$ is near 1300 m/s. The time of bubble degreasing from the initial size to ultimate size $R^* = 0.510\text{-}5 \text{ m}$ is $t_g = 0.6\text{-}0.71 \text{ e-}06 \text{ s}$. The steam temperature may be more than 1500 °K, [2-4]. If these processes take place near construction surface, in accordingly with loss particularly possibilities to resistance of deformation erosion grooves appear.

Basic equations

for deformable damageable medium (1) and liquid (2) with interface surface S_c fig.1, [5]

$$\begin{aligned} \rho_{,t} + \text{div}(\rho * \mathbf{V}) &= 0; & \rho(\rho * \mathbf{V})_{,t} + \text{div}(\rho * \mathbf{V}^2 + \boldsymbol{\sigma}) - \rho * \mathbf{F} &= 0; \\ \mathbf{e}_{,t} + \text{div}(\mathbf{e} + \boldsymbol{\sigma} - \mathbf{q}) * \mathbf{V} + \mathbf{Q}_{,t} &= 0; \boldsymbol{\sigma} = -\mathbf{p} * \mathbf{I}; & \mathbf{e} &= \rho * \chi + \frac{1}{2} \rho (\mathbf{v}^i)^2; \\ \text{artificiality viscosity } \mathbf{q} & & \text{Clausius - Duheme inequality.} & \\ \mathbf{p} = A \left(\frac{\rho}{\rho_0} - 1 \right) + B \left(\frac{\rho}{\rho_0} - 1 \right)^2 + C \rho \varepsilon & & \mathbf{p} = A \left(\frac{\rho}{\rho_0} - 1 \right) \mathbf{p} > -\mathbf{p}^* & \\ \mathbf{v}^1 \mathbf{n} = \mathbf{v}^2 \mathbf{n} & & \mathbf{p} = -\mathbf{p}^* & \mathbf{p} \leq \mathbf{p}^* \\ & & \mathbf{p}^1 \mathbf{n} = \mathbf{p}^2 \mathbf{n} & \\ \sigma_{jk} = -p \delta_{jk} + S_{jk} (j, k) = 1, 2, 3 & & S_{jk}^{\nabla} = \frac{\partial S_{jk}}{\partial t} - S_{jr} \omega_{rk} - S_{kr} \omega_{rj} & \\ \mathbf{p}(\mathbf{U}, \mathbf{e}) = \mathbf{p}_-(\mathbf{U}, \mathbf{e}) + \mathbf{p}_+(\mathbf{U}, \mathbf{e}) & & \mathbf{e} = \mathbf{e}_- + \mathbf{e}_+ & \\ \mathbf{p}_+(\mathbf{U}, \mathbf{e}) = \frac{\Gamma \mathbf{e}}{\mathbf{U}} & & \mathbf{p}_-(\mathbf{U}, \mathbf{e}) = \frac{d\mathbf{e}}{d\mathbf{U}} & \end{aligned}$$

A ductile behavior damageable structural material is similar process in viscous gas bubbles liquid, [1, 6].

Methods of numerical simulation

The numerical modeling of appreciably nonlinear behavior deformable damageable medium and liquid requires a using complex scheme numerical integration. The step time integration Δt is founded by use special criterions or CFL stability requirement, [7]. In respect to the modeled phenomena measure the shell - channel wall - can be represented as half medium to which is connected the corresponding part of liquid. The

cumulative liquid stream can be represented as radius R^* circle cylinder, variable velocity $V^*(r) = V_o^* \frac{(R^*)^2}{r^2}$

[2], along its length r , where V_o^* -bubble wall speed.

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COMPUTATION RESULTS

Dynamic half medium reaction for foregoing loading cases

It was considered two load cases: 1) *liquid is moistened damageable medium*. Propose that liquid velocity is zero on interface between them. It was found shock wave in liquid, located between destroyed bubble's wall

$R^* = 2.510 \cdot 10^{-5} \text{m}$ and medium surface with distance $r = 9.810 \cdot 10^{-5} \text{m}$, $(r/R^* = 3.92)$. The medium surface was loaded

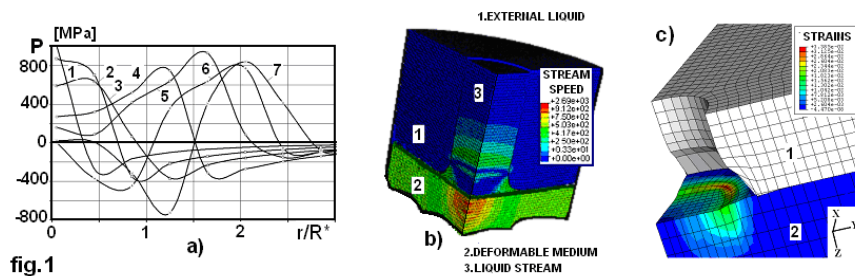
by pressure vs time. 2) *liquid is not moistened damageable medium*. Propose that liquid pressure is zero on interface between them. It was found shock wave in water, located between bubble's wall $R^* = 5.0 \cdot 10^{-5} \text{m}$ and

medium surface with distance $r = 9.55 \cdot 10^{-5} \text{m}$, $(r/R^* = 1.91)$. The medium surface was loaded by impact of moving

with the constant velocity $V_0^* = 400 \text{m/s}$ limited length stream. If steam bubble locates on medium surface (has the common part of wall) then the external loading can be represented as impact by unlimited length stream.

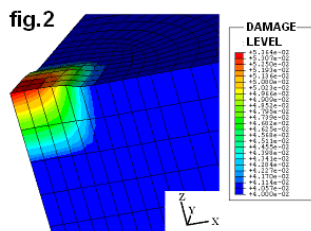
The liquid unlimited length stream impact. The stream liquid moves to the deformable half medium with the velocity $V^*(r)$, where $R^* = 5.0 \cdot 10^{-5} \text{m}$, $V_0^* = 1000 \text{m/s}$. As a result the complex wave processes arise in liquid

stream and in liquid around it. The maximum deformation locates along boundary loading square (fig.1).



Its quantity average $\varepsilon \sim 0.1$, when material resistance to deformation do not depend from heating, and - $\varepsilon \sim 0.25$ in opposite case at time moment $t = 5.0 \cdot 10^{-8} \text{s}$. Thus, the combination mechanics and heat loading will be fractured of shell material by way of erosion grooves.

The Impulsive pressure action $P(t)$. fig.2. When heating of material is omissible, then this loading do not leads to an appreciably variation of it state. The variation shell material resistance to deformation as a result of it local heating conduce to its tension located on loading square at a depth of $\sim 3.0 \cdot 10^{-5} \text{m}$. There is plastic flow in term of all strained material volume. And as result of this its porosity increases. The maximum deflection, deformation and porosity locate in the centre of loading square. Its quantities average $\delta = 3.3 \cdot 10^{-7} \text{m}$ in direction of loading, $\varepsilon \sim 0.018$ at time $t = 2.8 \cdot 10^{-8} \text{s}$, $V_p \approx 6\%$ at time $t = 1.0 \cdot 10^{-6} \text{s}$.



The liquid limited length stream impact. It considers as the special case of the liquid with unlimited length. At beginning $t=0$ liquid stream with length $L = 5.0 \cdot 10^{-5} \text{m}$ begin to move from bubble wall $R^* = 5.0 \cdot 10^{-5} \text{m}$ to the deformable

half medium with the constant velocity $V_0^* = 400 \text{m/s}$. This loading does not lead to fracture medium material. But if bubbles destroy are considered as association in unit of liquid volume in this case fractures may be.

CONCLUSION

The compression and destroy steam bubbles lead to the transitional wave processes in liquid. Its parameter average quantities are pressure is near 1.0 GPa, velocities are near 1300 m/s, temperature is near 1500 °K. The character length and duration each of them are the ultimate bubble size and specific time it's variation. The combination mechanics and heat loading lead to fracture of shell material. An erosion grooves appear.

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